

# A deconvolution method for the mapping of residual-stresses by X ray diffraction

Application to the validation of process simulations

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# A deconvolution method for the mapping of residual-stresses by X-ray diffraction

- **Introduction**
- **Principle of the method**
- **Application to SPD process (RCS)**
- **Conclusion**



# Introduction

## Context of this study : the XRD method for residual stresses

- XRD: accurate method for in-depth measurements of residual stresses
  - High accuracy and non-destructive way to determine residual stresses
  - Stress gradients in depth with a very good precision and resolution: with electro-polishing or multi-reflection grazing incidence (*M. Marciszko et al. 2014*)
- ...but: Inaccurate method in the presence of high surface stress gradients
  - Stress obtained by XRD : convolution of the local stress over the irradiated area (*Kahloun et al., 1994; Hennion et al., 2000; Kahloun et al., 2014*)
  - The irradiated area cannot be reduced because it must contain enough crystallites to be statistically representative

→ In the presence of high lateral stress gradients inherent averaging effects are expected to occur

# Introduction

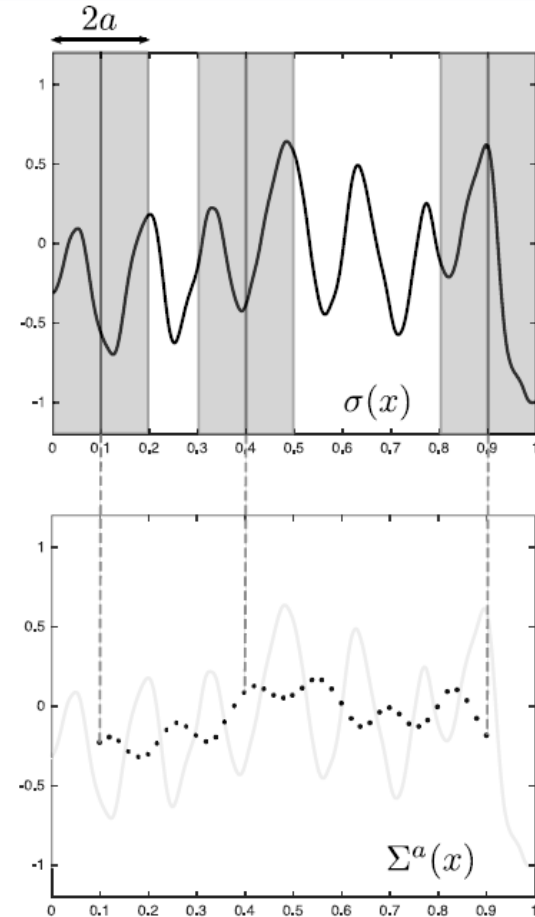
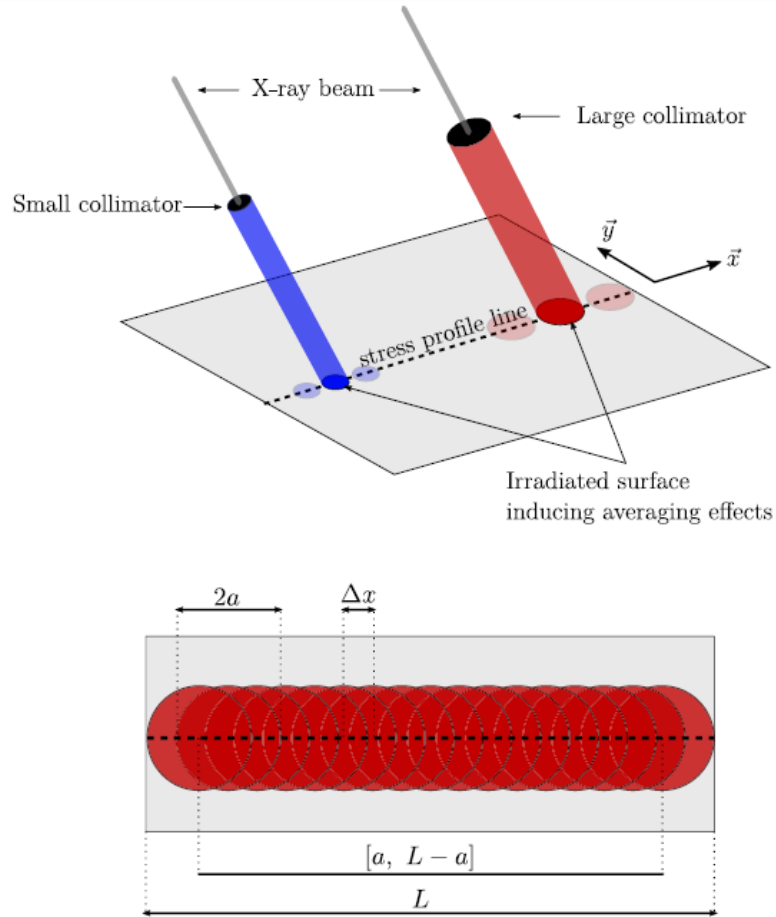
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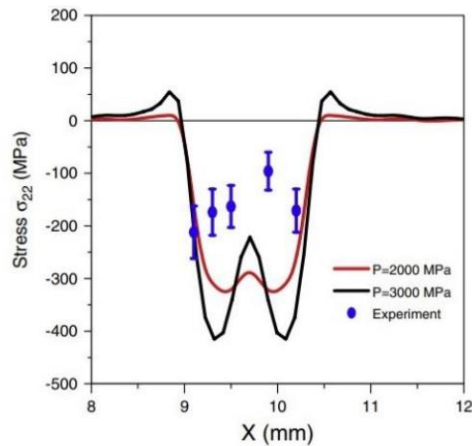
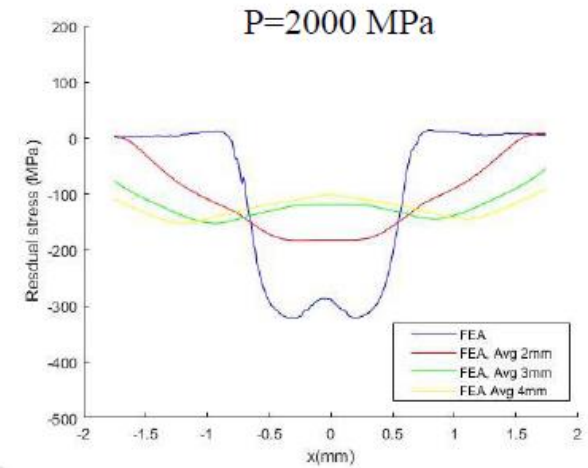
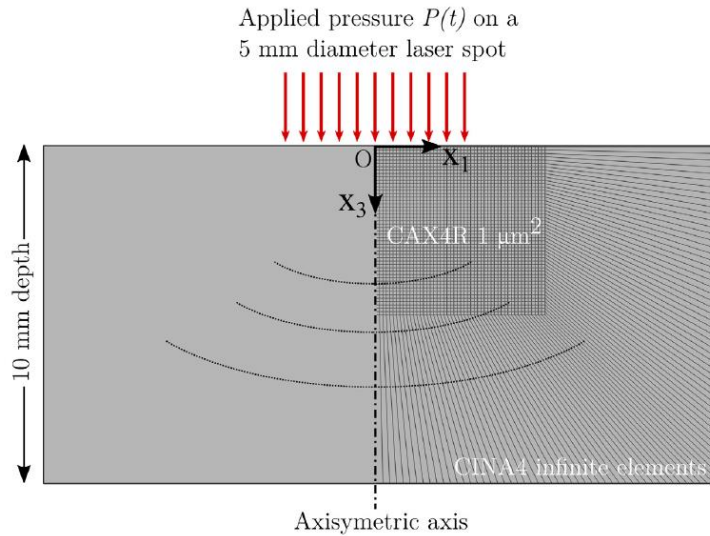
# Introduction

## On the importance of averaging effects in XRD measurements

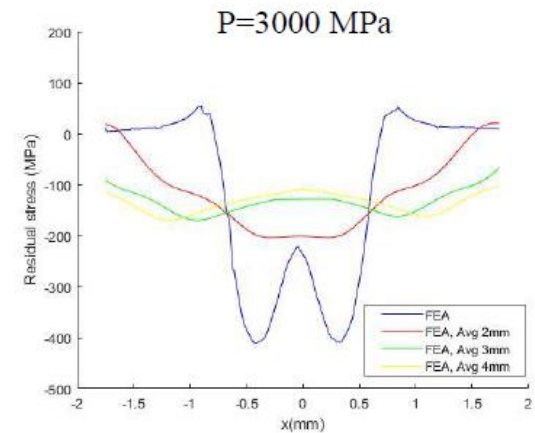


# Introduction

## A test case : residual stresses in Laser Shock Peening



(P.Peyre et al. 2015)



# A reconstruction method of residual stresses based on XRD

## Principles of the method (1D case)

- Reconstruct the local stress field  $\sigma$  from an average measure  $\Sigma^a$  (over the irradiated area) obtained by XRD

$$\Sigma^a(x) = \frac{1}{2a} \int_{x-a}^{x+a} \sigma(u) du$$

- Using a regular measurement grid and expressing this integral with a discrete rule, one can establish a linear relation between the pointvalues of  $\sigma$  and  $\Sigma^a$

$$\Sigma^a = \mathbf{R}^a \sigma$$

- (Approximate) inversion of this system leads to the reconstructed stress field

$$\sigma = (\mathbf{R}^a)^+ \Sigma^a$$

# A reconstruction method of residual stresses based on XRD

## Practical implementation

- In practice, several issues are observed on the reconstruction due to:
  - The presence of noise on the measurements
  - The low number of equations (the system is underdetermined)
- Improvements of the method include
  - Automatic smoothing of the experimental datasets
  - Use of several collimator for the measurements (inducing several average datasets) to evaluate the averaging effect
- The method is then based on an automatic sampling (using a robot)  
→ 1D line profile
- Extension from 1D to 2D mapping using regular sampling in two directions



# Application to the reconstruction of 1D stress profiles

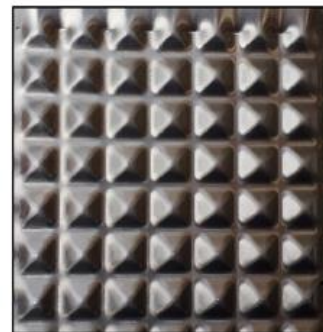
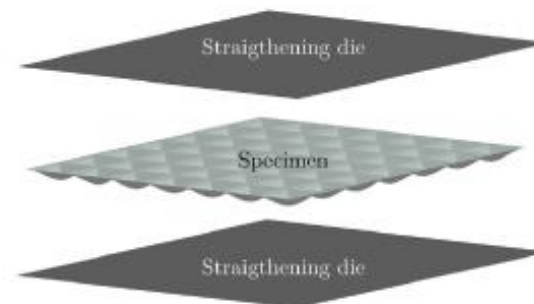
## Application to simulated data (reference case)

- Method is first assessed in a reference case with simulated data: FEM simulation of the RCS process (*P. Tajdary et al., 2021; L. Morin et al., 2021*)

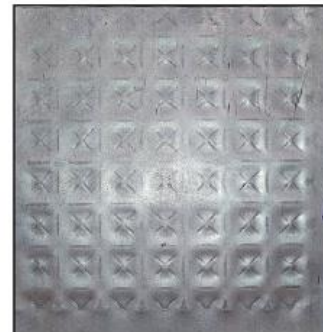
RCS Step 1: Corrugation



RCS Step 2: Straightening



Specimen after corrugation



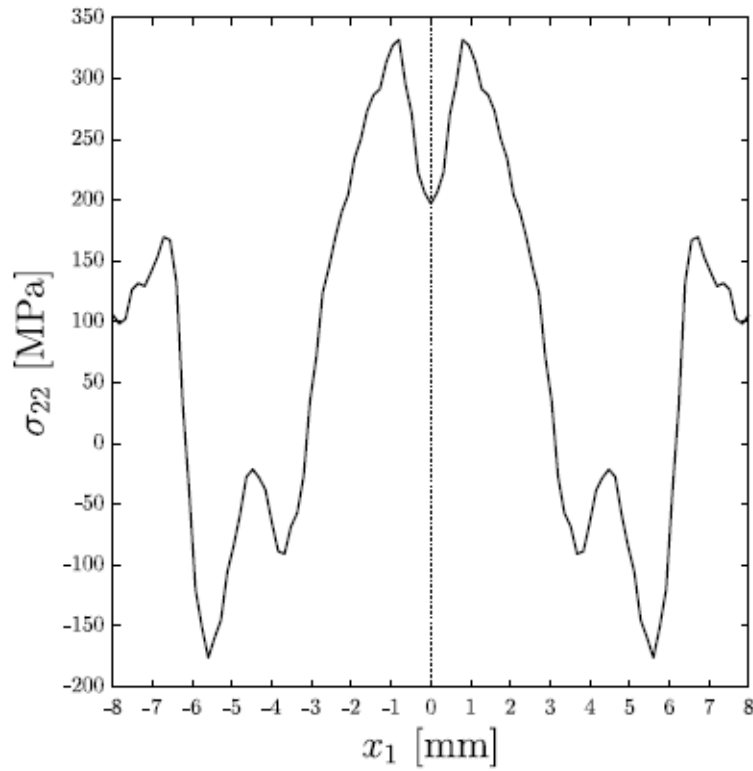
Specimen after straightening

1-Pass RCS with aluminum alloy AA6061-T6

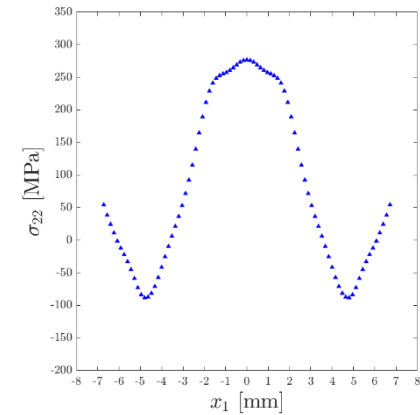
# Application to the reconstruction of 1D stress profiles

## Application to simulated data (reference case)

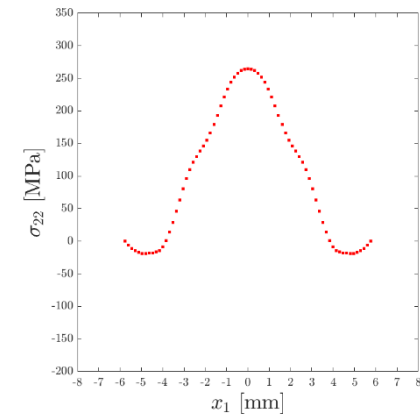
- Average datasets are constructed from the local profile using two collimators (Irradiated area diameter 2.5 mm and 4.5 mm)



2,5 mm



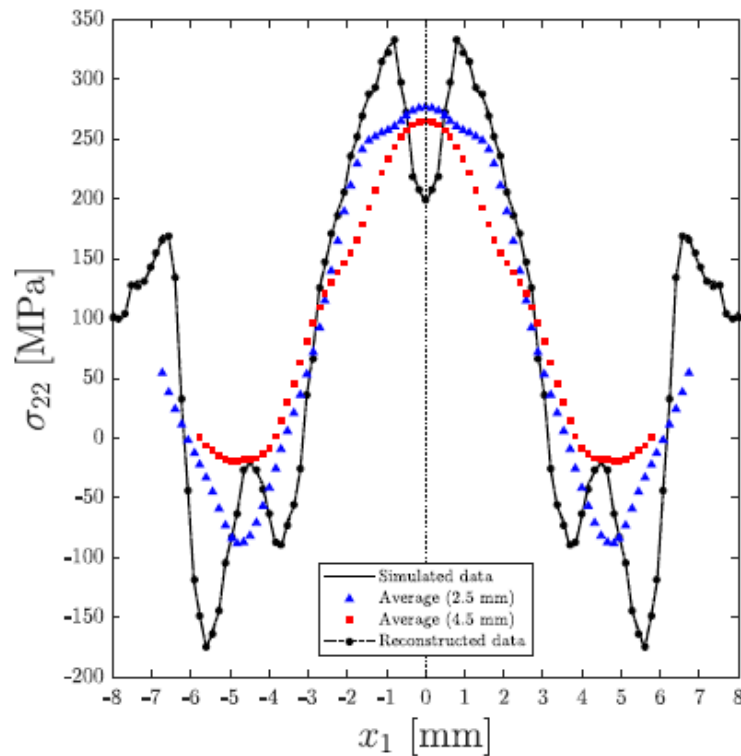
4,5 mm



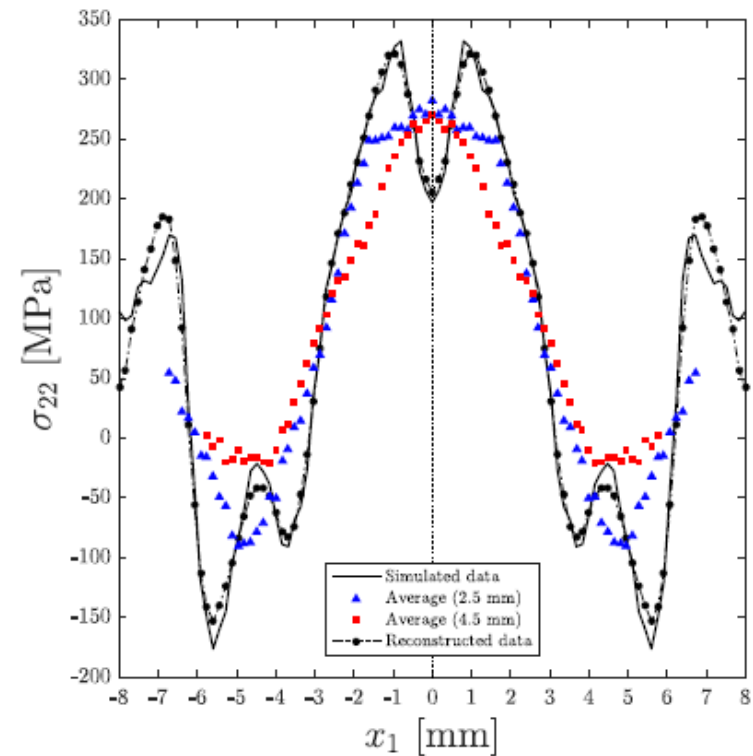
# Application to the reconstruction of 1D stress profiles

## Application to simulated data (reference case)

Reconstructed data is calculated from the average datasets and compared to the initial reference solution



without noise



with noise on the datasets

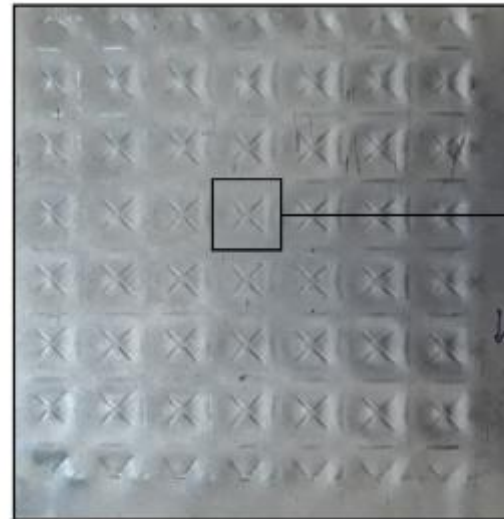
# Application to the reconstruction of 1D stress profiles

## Application to experimental data

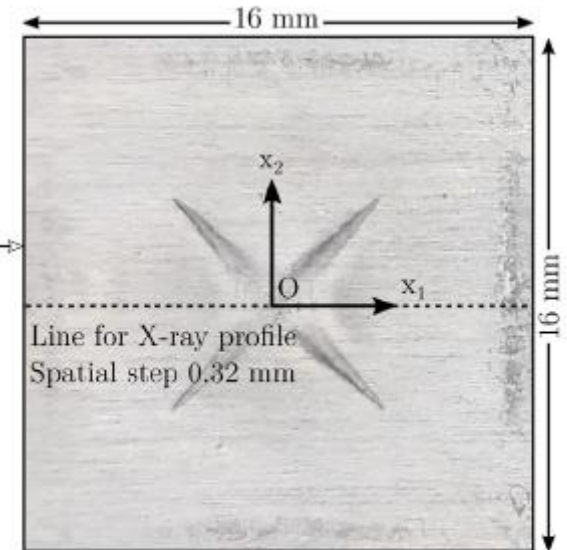
- Method is applied to experimental measurements of RCS



Specimen after corrugation



Specimen after straightening

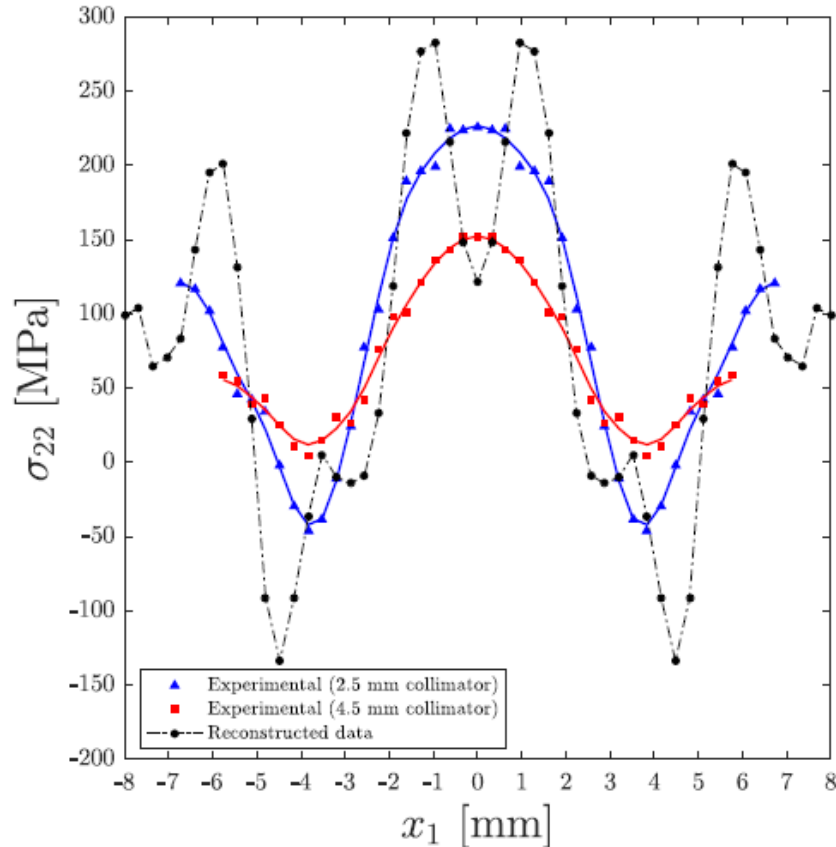


Elementary pattern considered for X-ray measurements

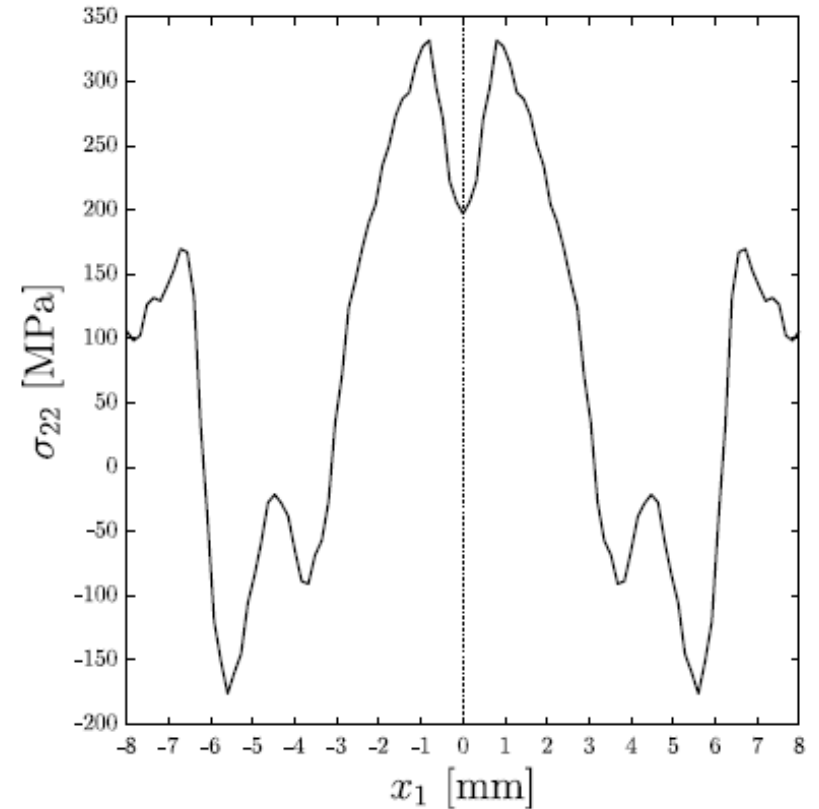
- Spatial step : 0.32 mm (50 points on the line)
- 2 collimators used : 2.5 mm and 4.5 mm diam.of irradiated surf.

# Application to the reconstruction of 1D stress profiles

## Application to experimental data



Experimental datasets and reconstructed stress

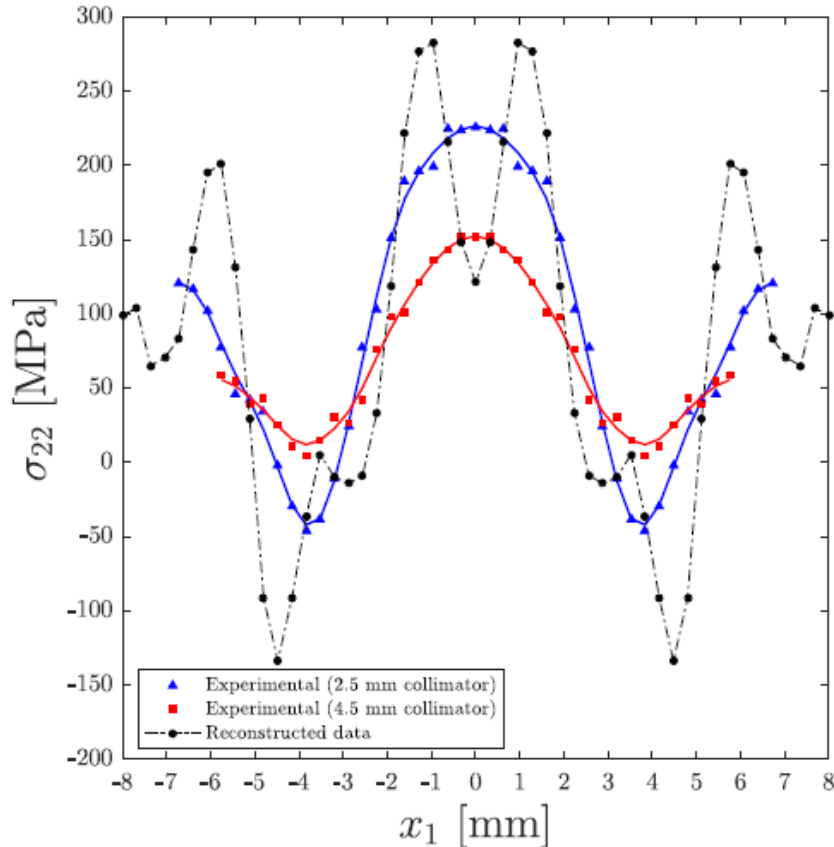


Numerical results for comparison

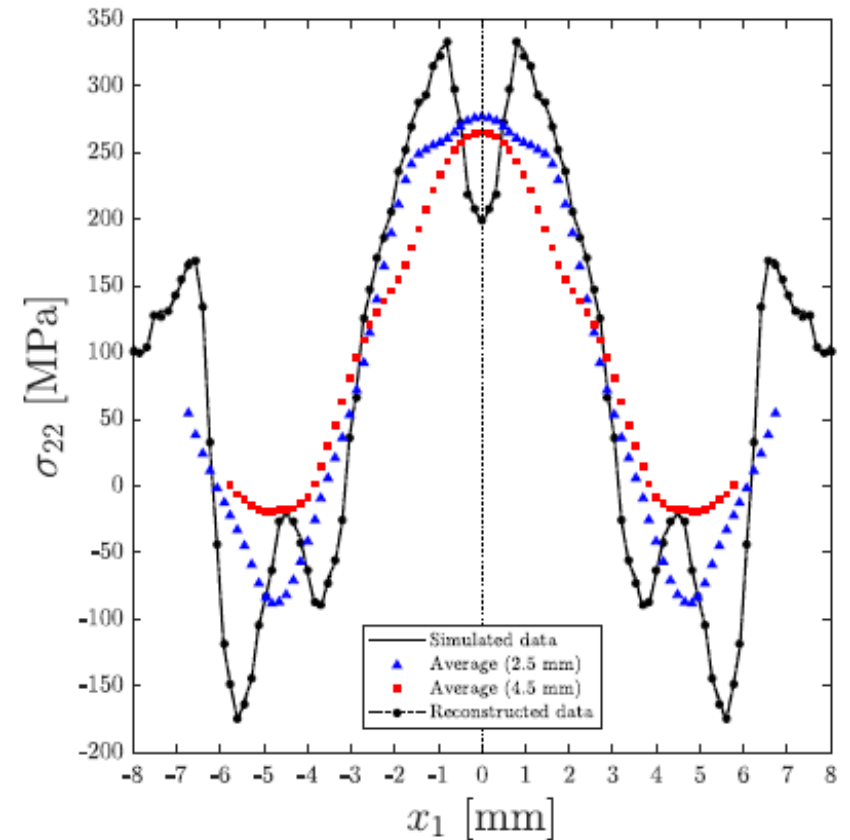
# Application to the reconstruction of 1D stress profiles

## Application to experimental data

Psi-tilt method: 2  $\phi$  and 13  $\psi$  per point



Experimental datasets and reconstructed stress

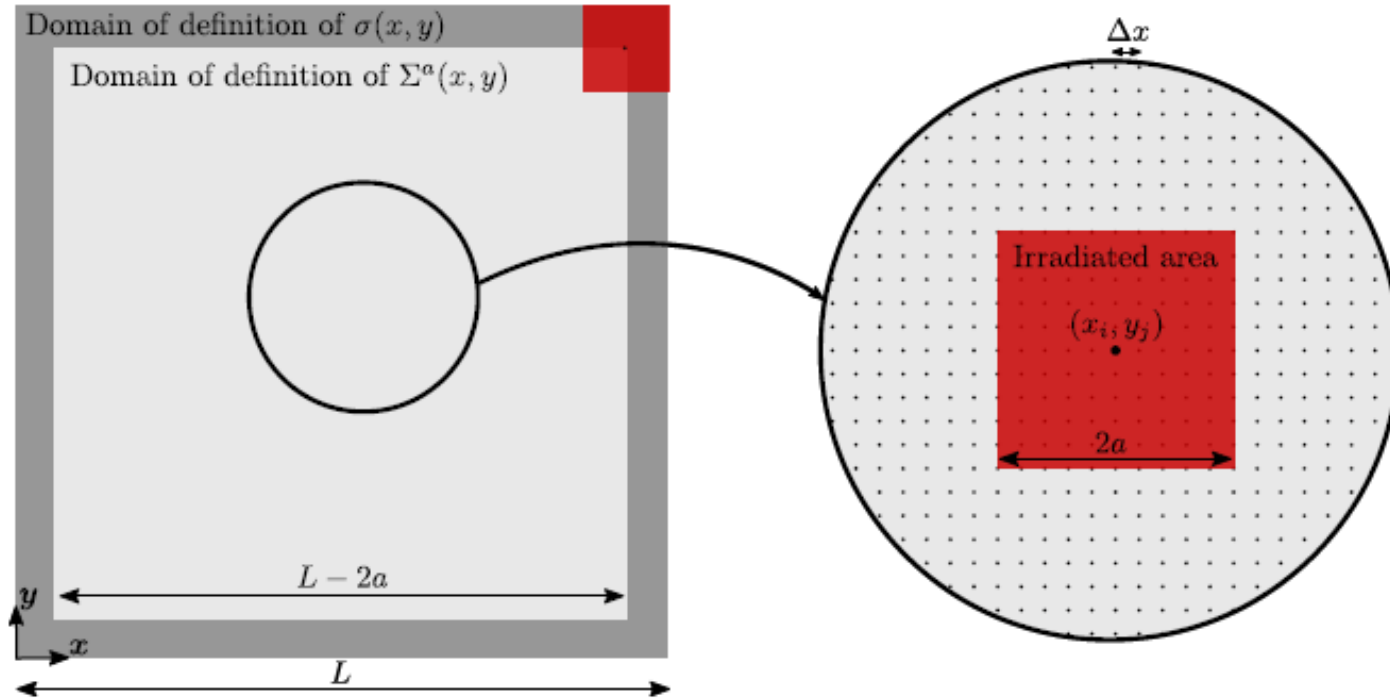


Numerical results for comparison

# Application to the reconstruction of 2D mapping

## Extension to 2D mapping

- Extension to 2D mapping using regular sampling in two directions

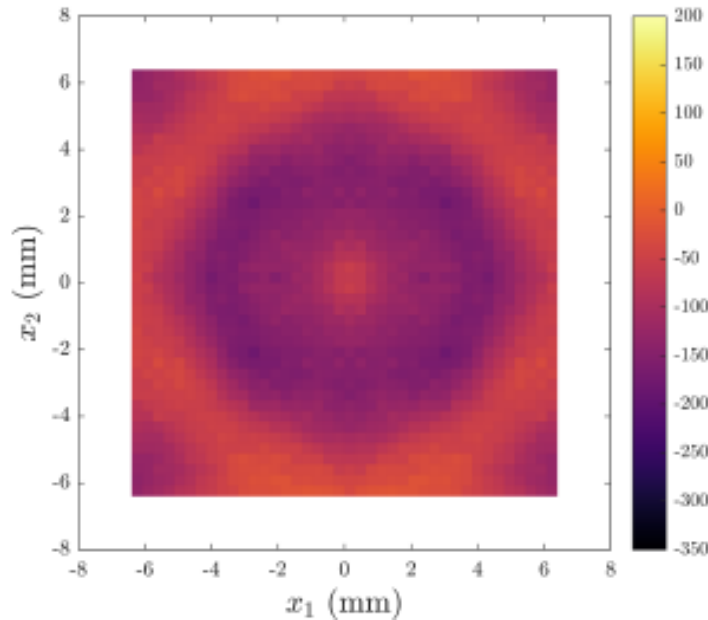


- Linear relation between local and average stresses can be also obtained

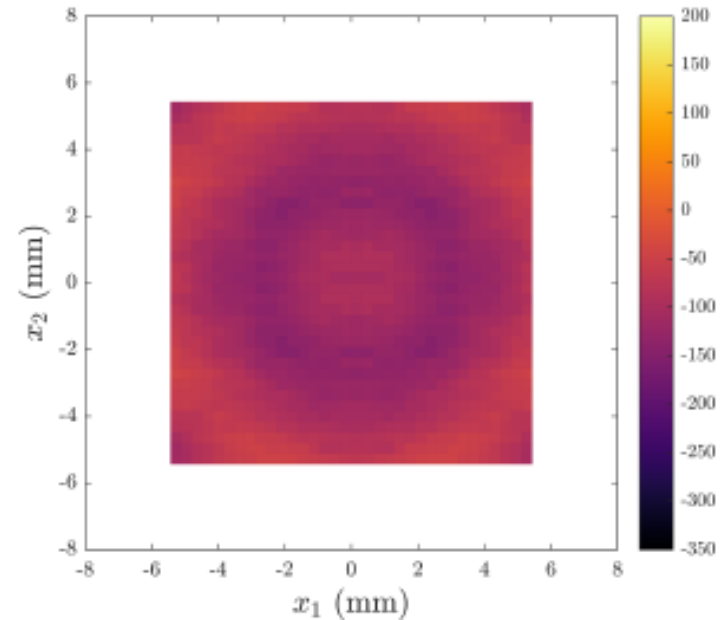
# Application to the reconstruction of 2D mapping

## Application to experimental data

- Application to a 2D mapping with 0.32 mm (2500 points)  
 $\sigma_{11} + \sigma_{22}$  from  $\varepsilon_{33}$ : one direction  $\phi = 0$  and 13  $\psi = 0$  per point



Average dataset with  $\phi 2.5$  mm collimator  
 $\sigma \in [-180, -13]$  MPa



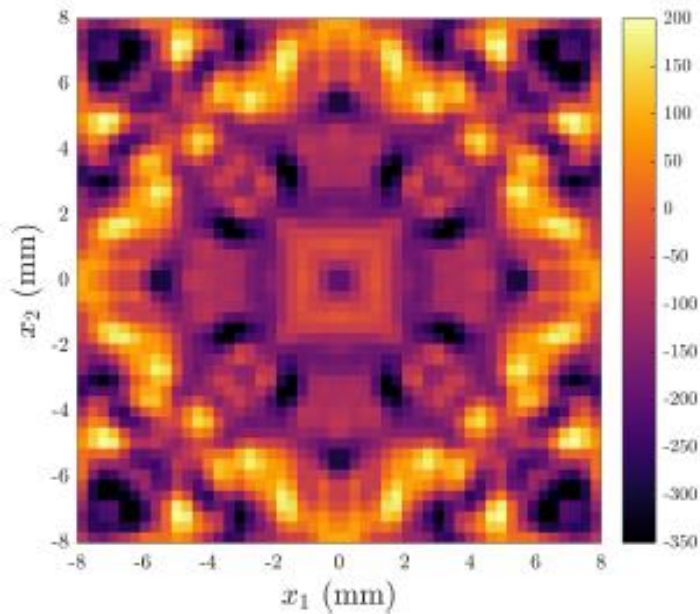
Average dataset with  $\phi 4.5$  mm collimator  
 $\sigma \in [-147, -44]$  MPa

- High averaging effects observed

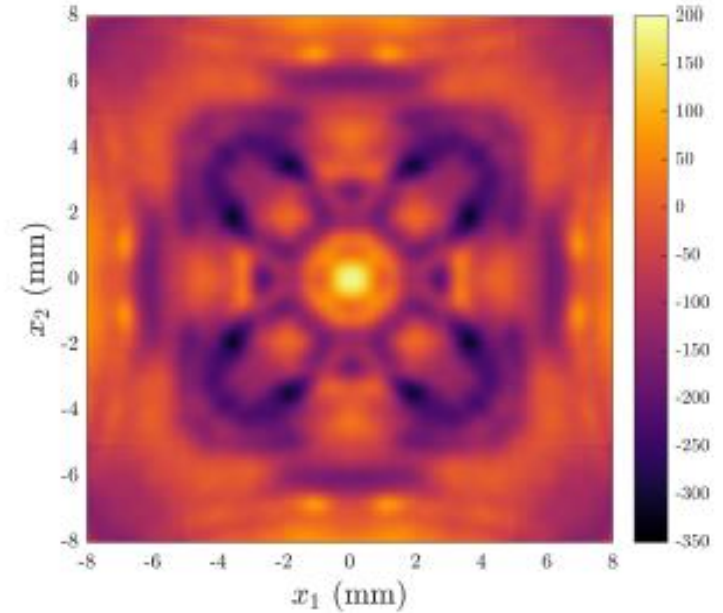


# Application to the reconstruction of 2D mapping

## Application to experimental data



Reconstructed field from XRD  
measurements



Local FEM  
Results

# Conclusion

- A deconvolution method was proposed to determine the surface profile of residual-stresses by X-ray diffraction with high spatial resolution.
- The XRD measurements were performed by using a robot diffractometer.
- It was successfully applied to specimen processed by RCS on one dimension and then extended to a 2D mapping.
- Despite requiring an extensive number of measurement points, this method is useful for validating FEM simulation models of processes inducing high-gradient surface stresses.