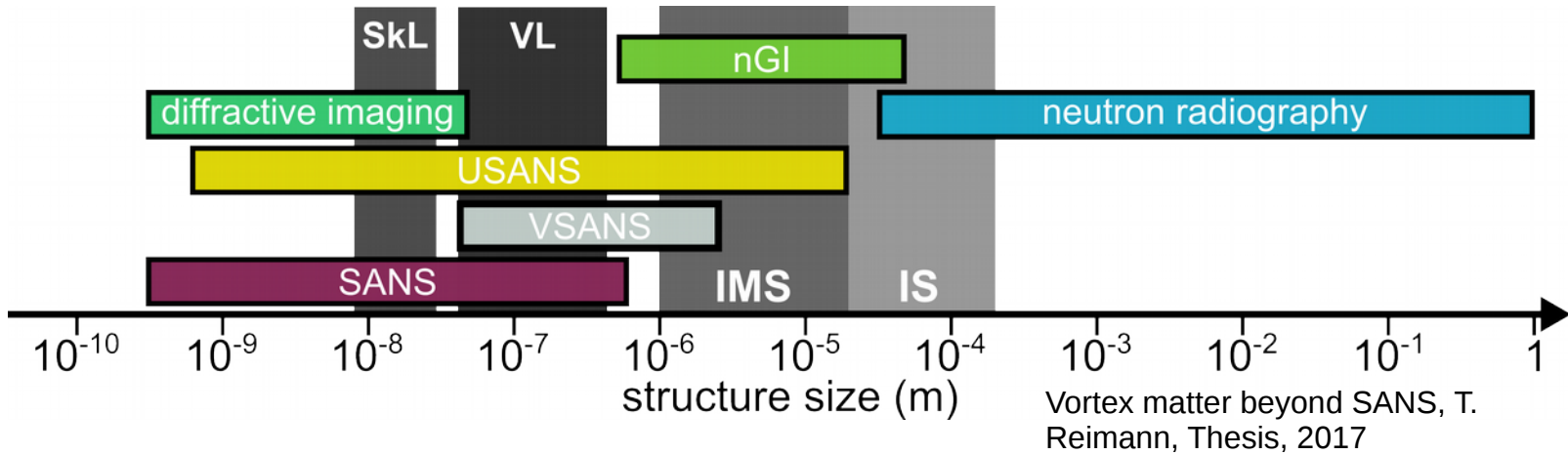


NEUTRON GRATING INTERFEROMETRY I

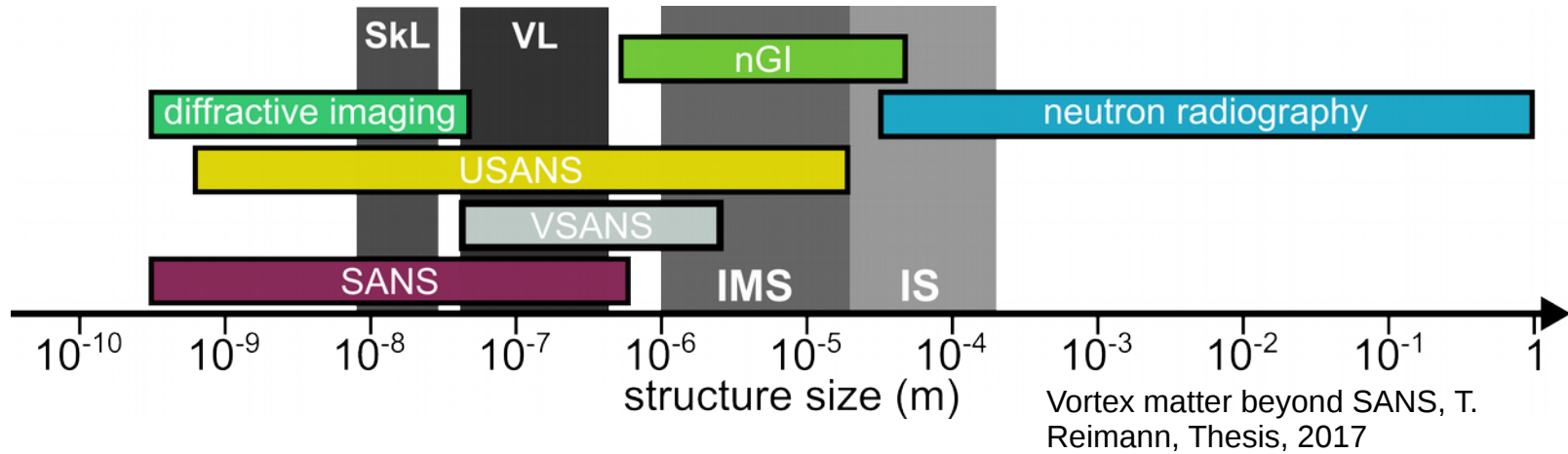
THEORY AND PRINCIPLES

Tobias Neuwirth

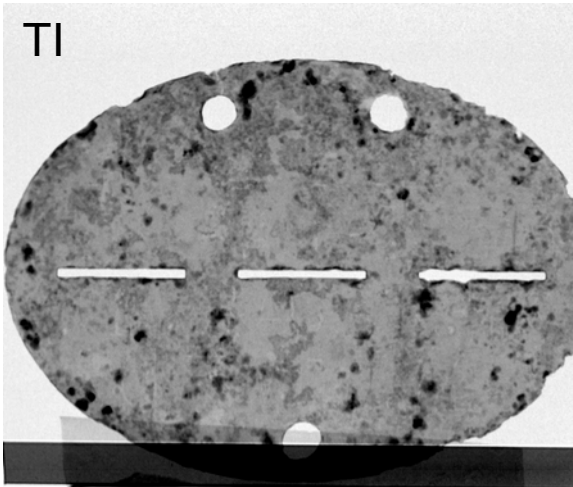
Why neutron grating interferometry?



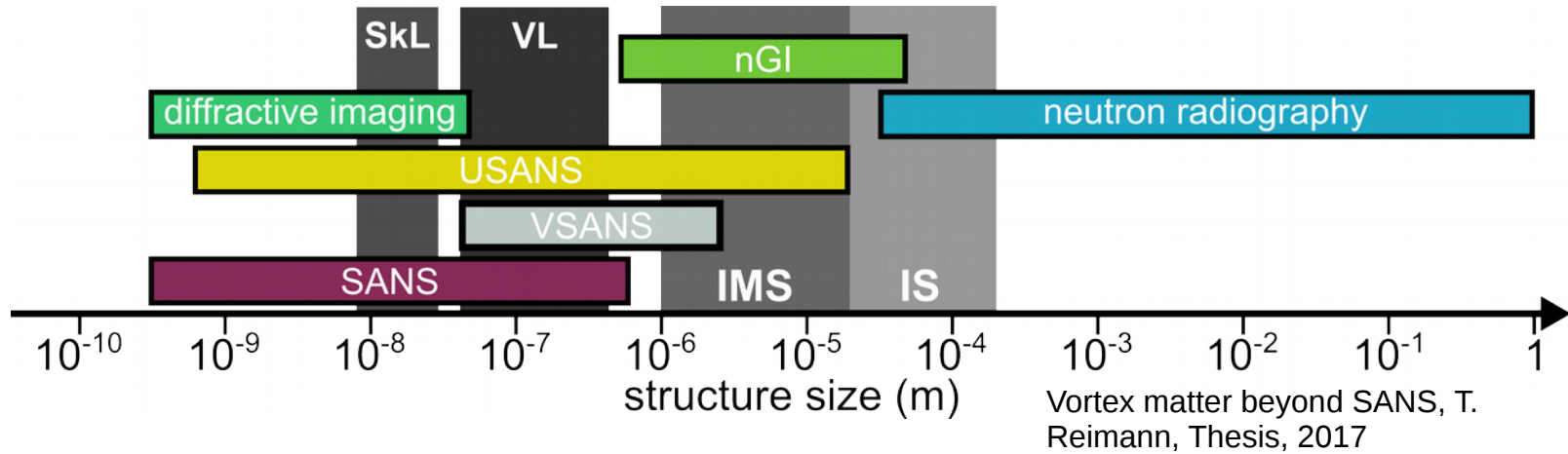
Why neutron grating interferometry?



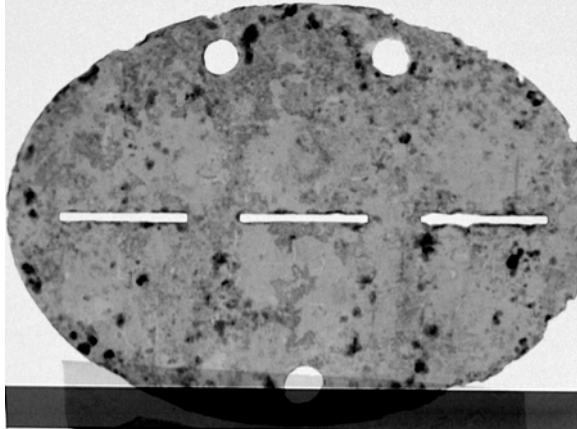
Tl



Why neutron grating interferometry?



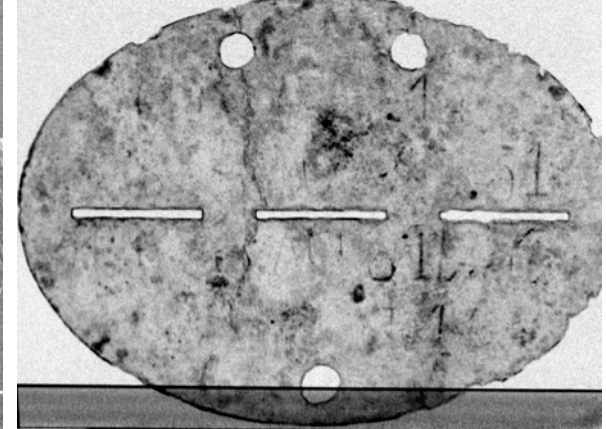
TI



DPCI



DFI

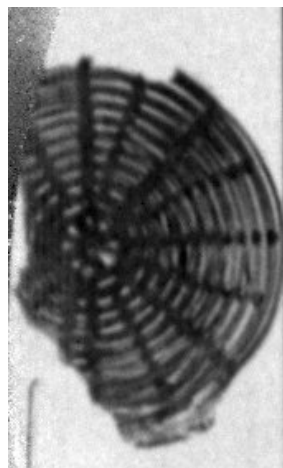
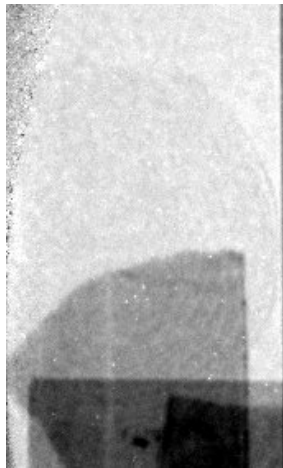


Why neutron grating interferometry?

qualitative

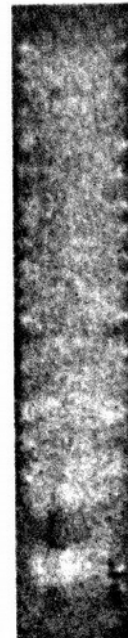
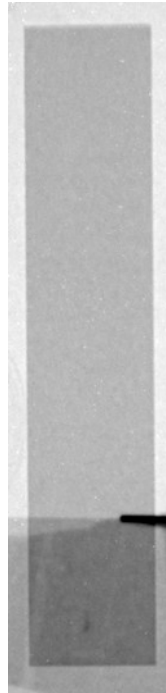
TI

DFI

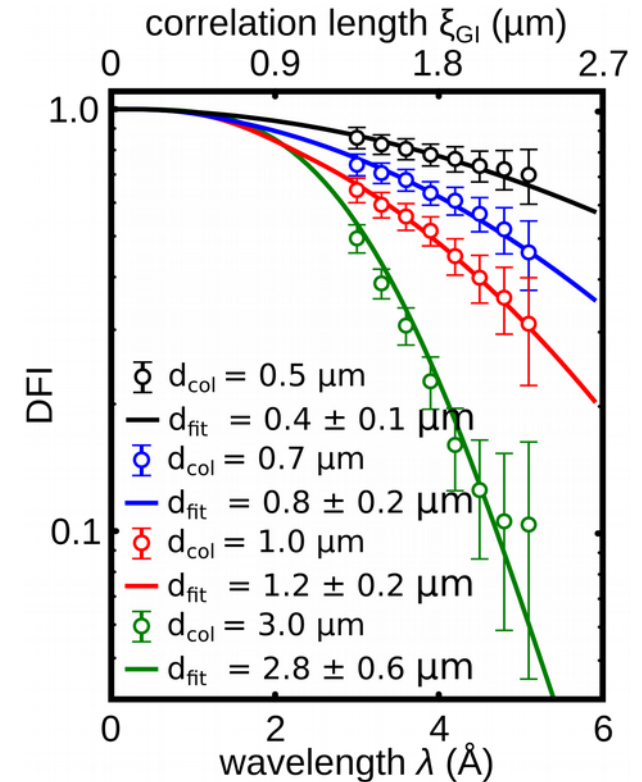


TI

DFI

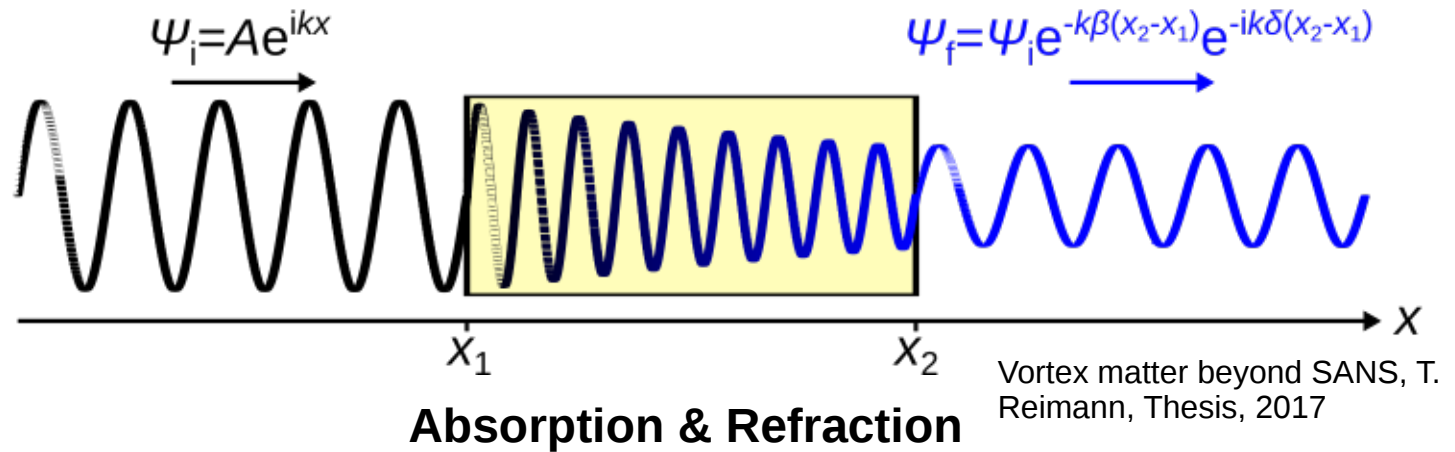


quantitative



Vortex matter beyond SANS, T. Reimann, Thesis, 2017

- **Interaction of neutrons with matter**
- **Principle of neutron grating interferometry**
- **Construction of an nGI**
- **Summary**

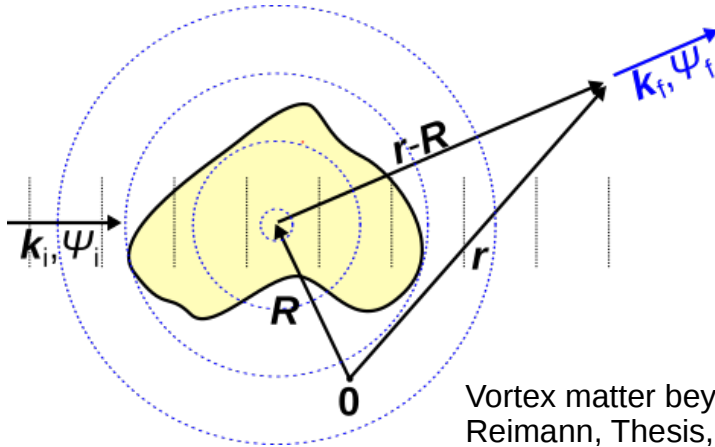


Vortex matter beyond SANS, T. Reimann, Thesis, 2017

$$T = \frac{I_f}{I_i} = \exp[-(\sigma_{\text{abs}} + \sigma_{\text{inc}}) Nt]$$

$$\Delta \Phi = -\lambda N b_c t$$

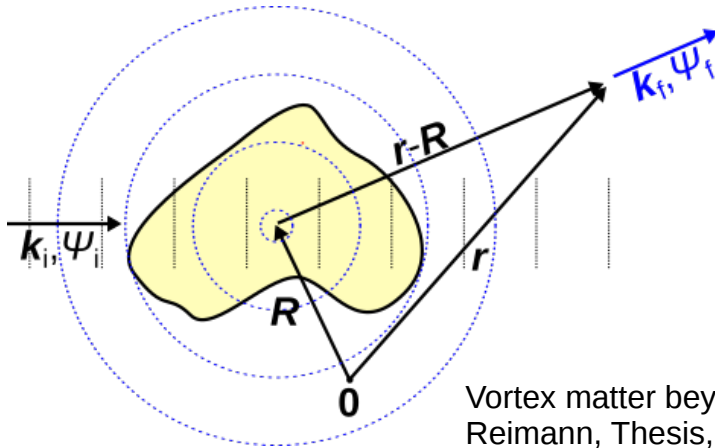




$$\Psi_f(k_f, r) = \exp(i k_i \cdot r) + \exp(i k_f \cdot r) f(q)$$

Basic scattering function

Vortex matter beyond SANS, T. Reimann, Thesis, 2017

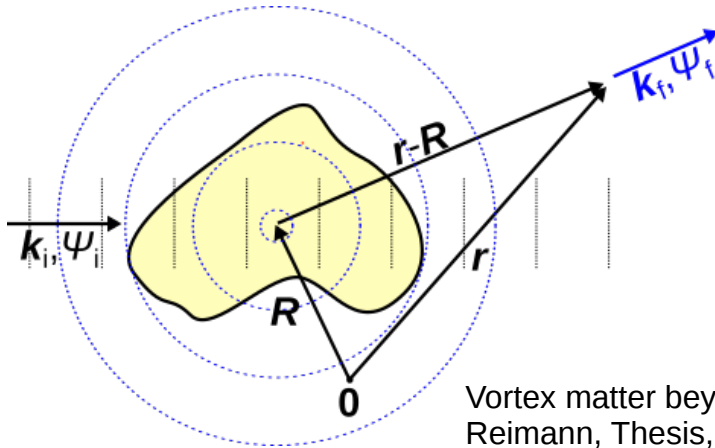


$$\Psi_f(k_f, r) = \exp(i k_i \cdot r) + \exp\left(\frac{i k_f \cdot r}{r}\right) f(q)$$

Basic scattering function

Vortex matter beyond SANS, T.
Reimann, Thesis, 2017

For neutron grating interferometry the scattering we are interested in the scattering under ultra-small-angles (USANS).



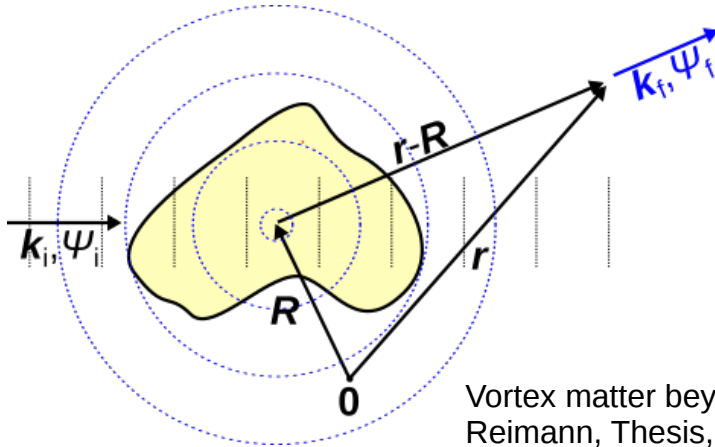
$$\Psi_f(k_f, r) = \exp(i k_i \cdot r) + \exp\left(\frac{i k_f \cdot r}{r}\right) f(q)$$

Basic scattering function

Vortex matter beyond SANS, T.
Reimann, Thesis, 2017

For neutron grating interferometry the scattering we are interested in the scattering under ultra-small-angles (USANS).

How do we analyse this scattering?



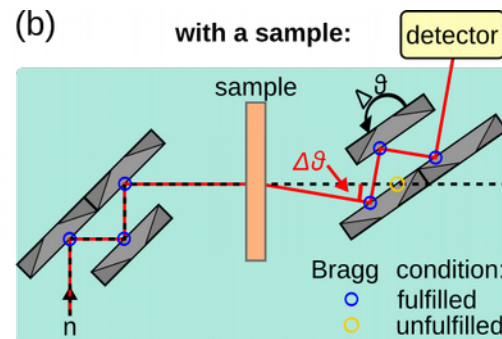
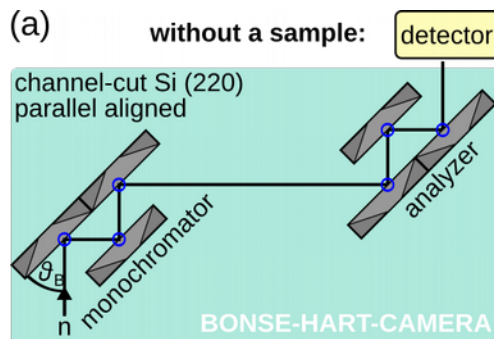
$$\Psi_f(k_f, r) = \exp(ik_i \cdot r) + \exp\left(\frac{ik_f \cdot r}{r}\right) f(q)$$

Basic scattering function

Vortex matter beyond SANS, T. Reimann, Thesis, 2017

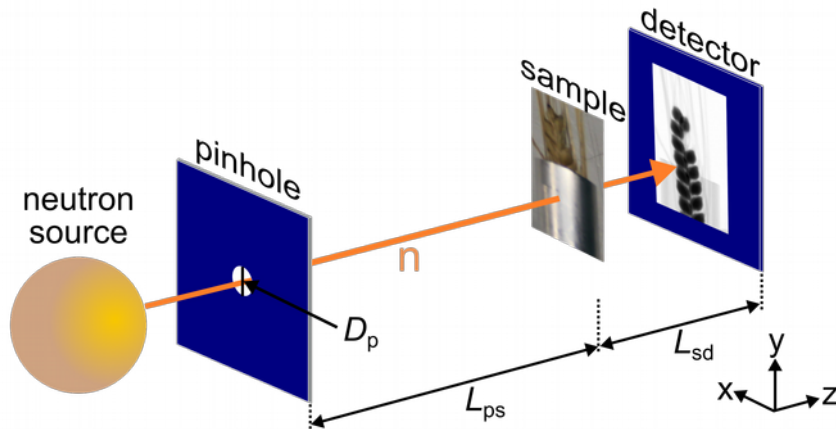
For neutron grating interferometry the scattering we are interested in the scattering under ultra-small-angles (USANS).

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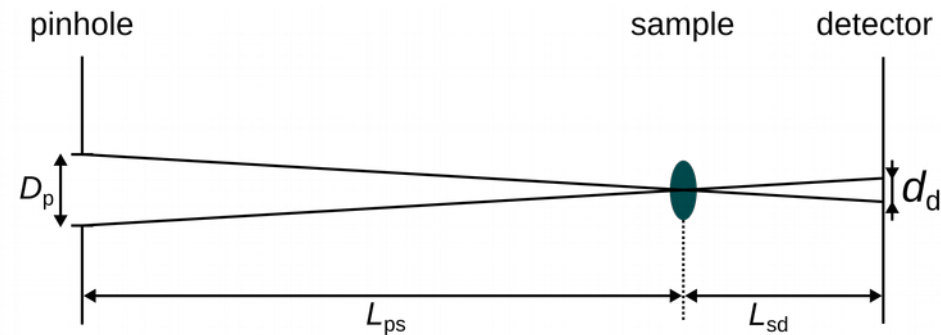


Vortex matter beyond SANS, T. Reimann, Thesis, 2017

Neutron radiography



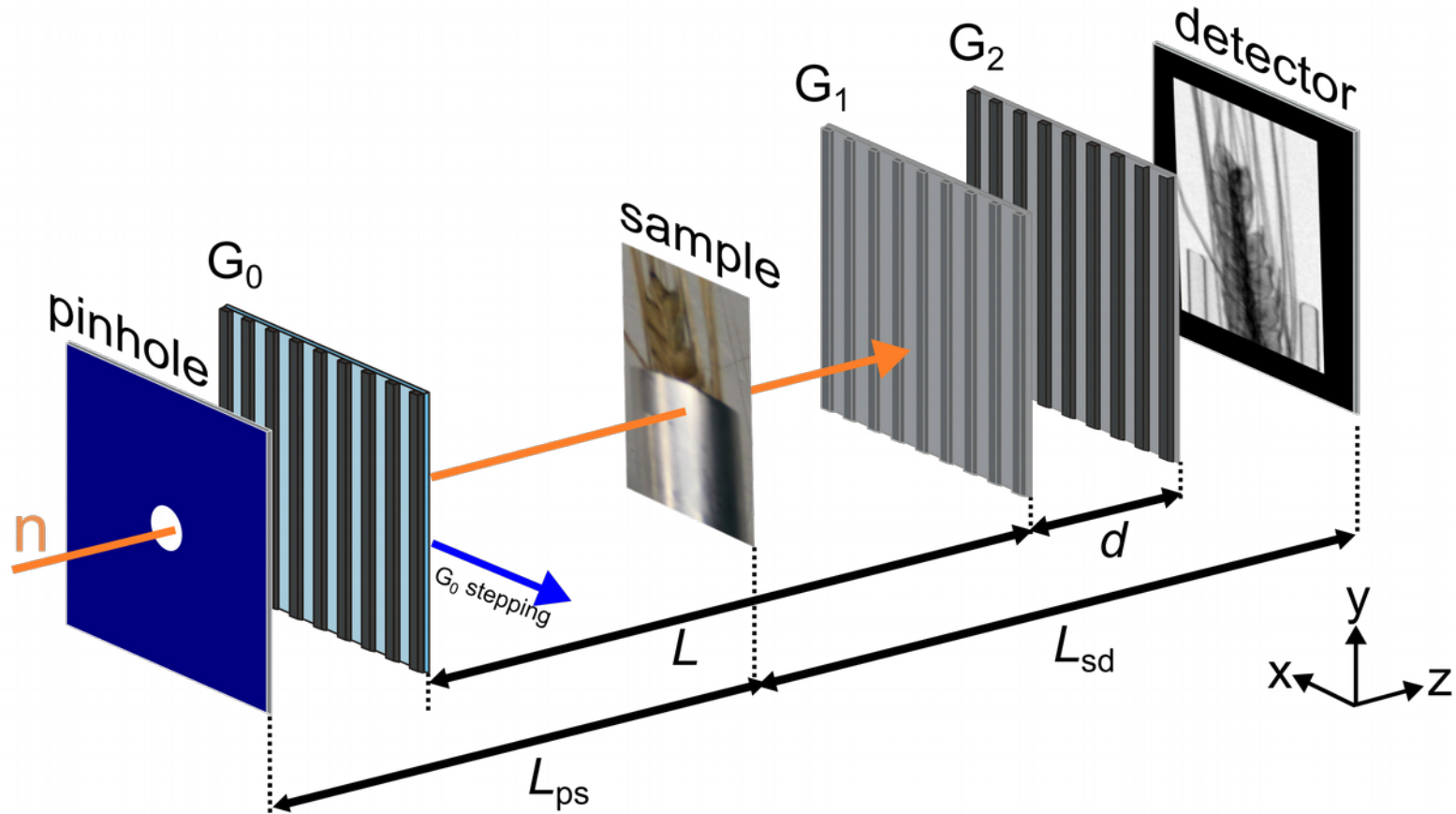
Geometric resolution



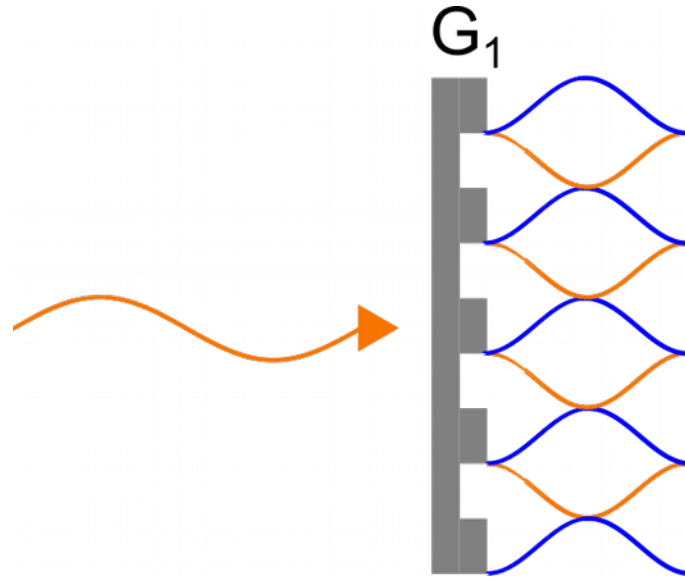
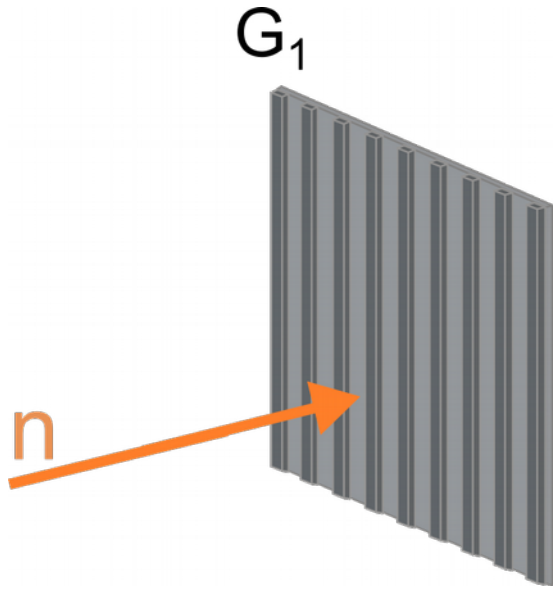
$$d_d = \frac{D_p}{L_{ps}} \cdot L_{sd}$$

- Analysis of the inner structure of a sample by analysing the absorption
- Resolvable structure size limited by geometric resolution, scintillator thickness and quality of the camera system

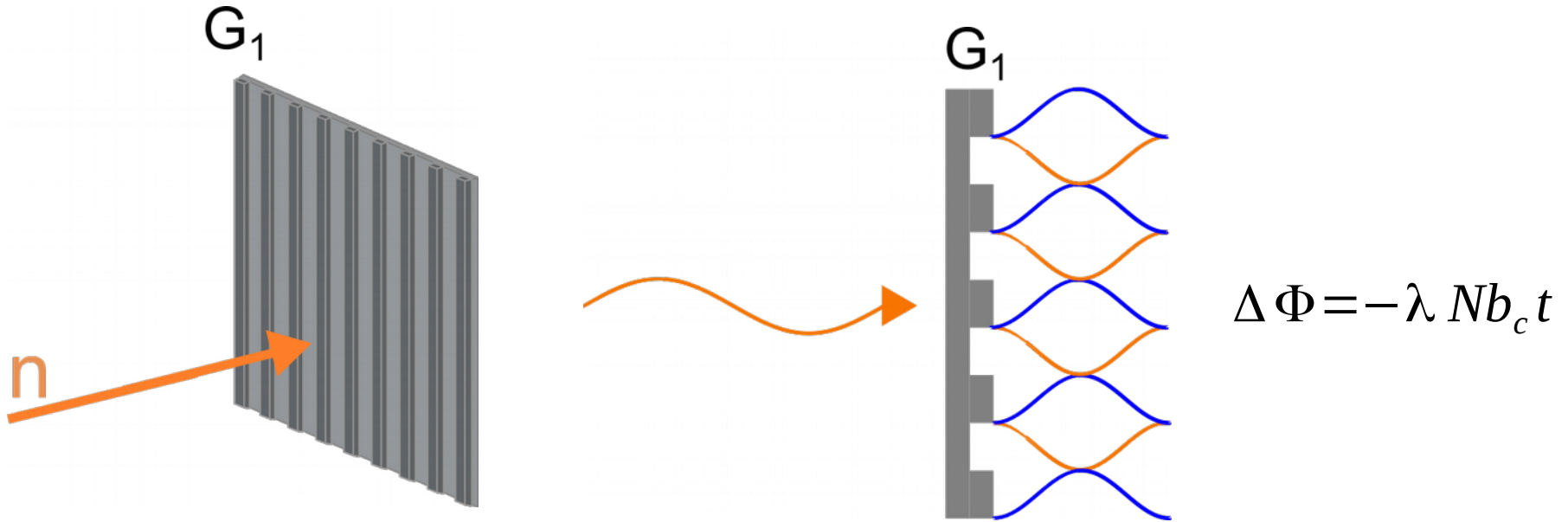
Neutron grating interferometer



G_1 – splitting the beam

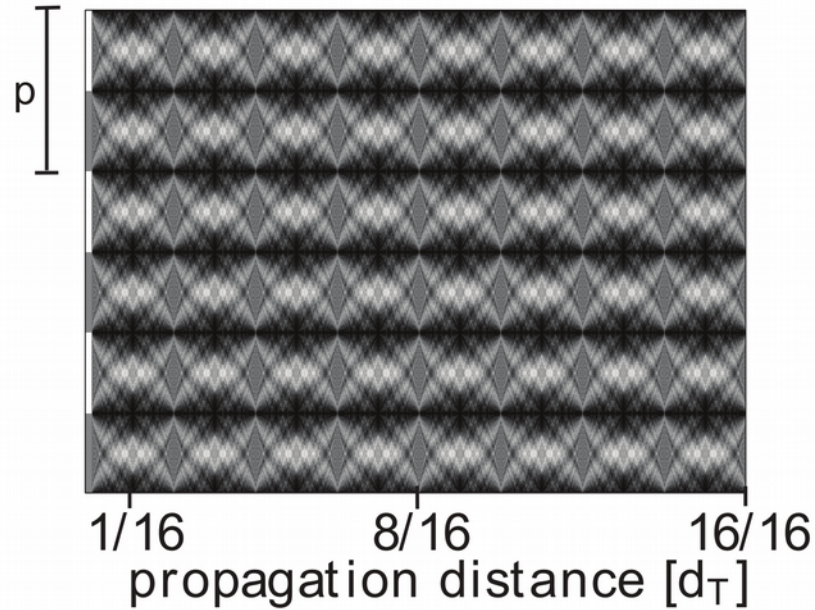


$$\Delta\Phi = -\lambda N b_c t$$

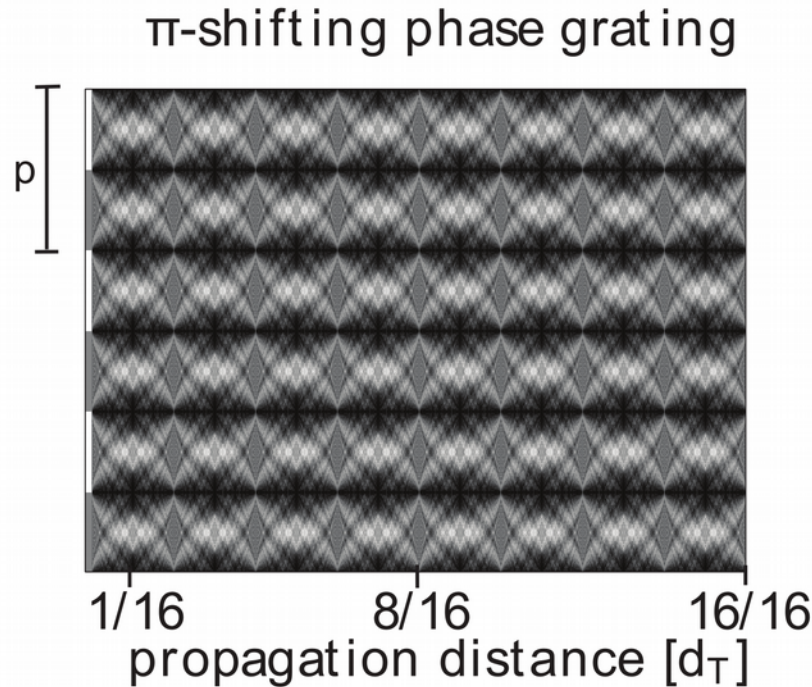


- Phase shift of the neutron when passing through G_1 dependent on the height of the grating and the wavelength of the neutrons
- Period of G_1 used in ANTARES $\approx 8 \mu\text{m}$

π -shifting phase grating



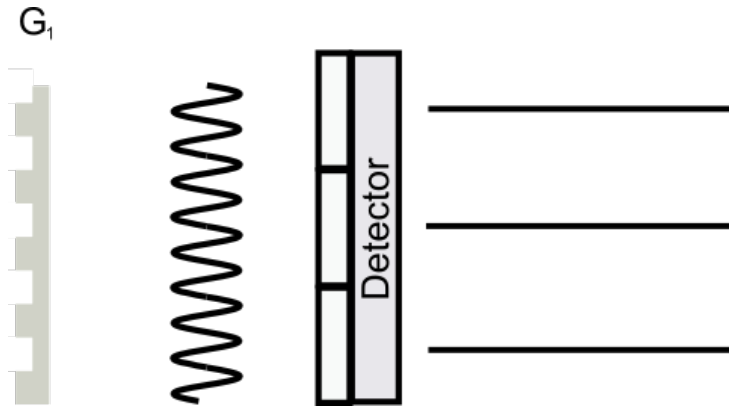
$$d_n = \frac{n}{16} d_T = n \frac{p_1^2}{8\lambda}$$

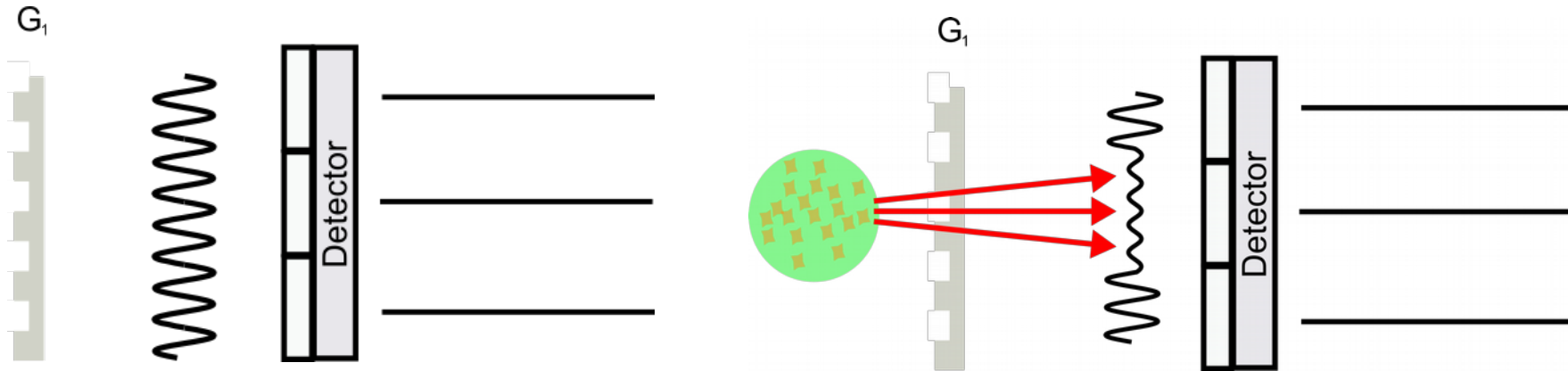


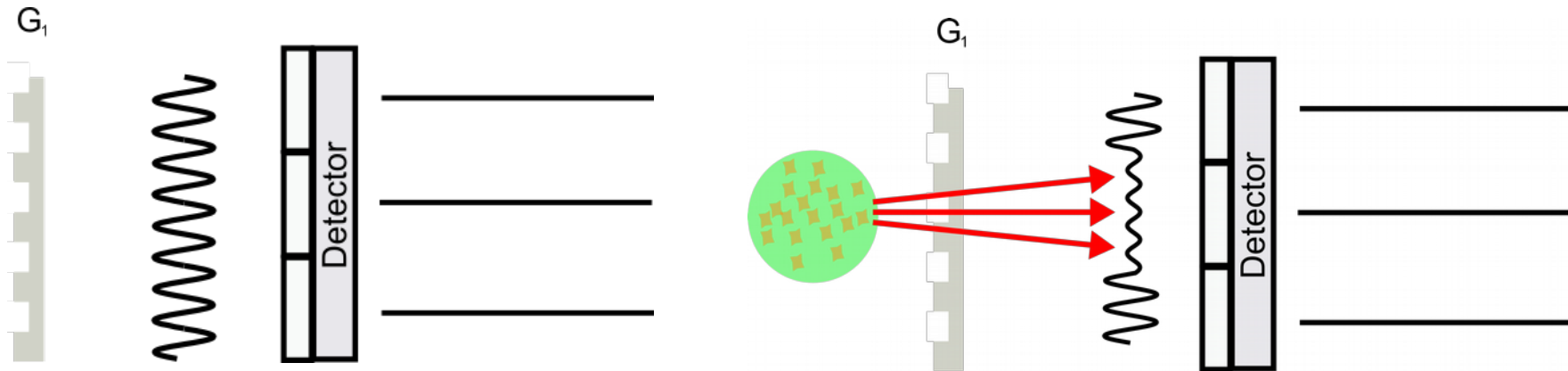
$$d_n = \frac{n}{16} d_T = n \frac{p_1^2}{8\lambda}$$

Contributions to the characterization of grating-based x-ray phase-contrast imaging, M. Chabior, Thesis, 2011

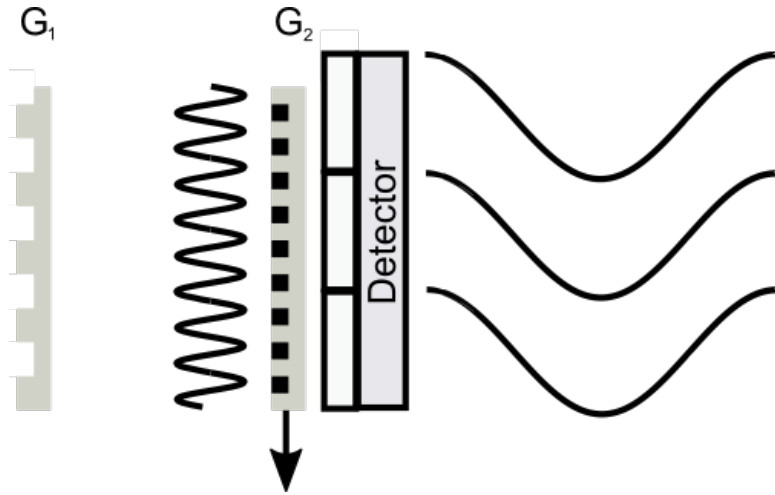
- Generation of a Talbot-carpet after G_1
 - Odd fractional Talbot distances result in a intensity modulation
 - Even fractional Talbot distances result in a phase modulation
- Intensity modulation has half the period of $G_1 \approx 4 \mu\text{m}$

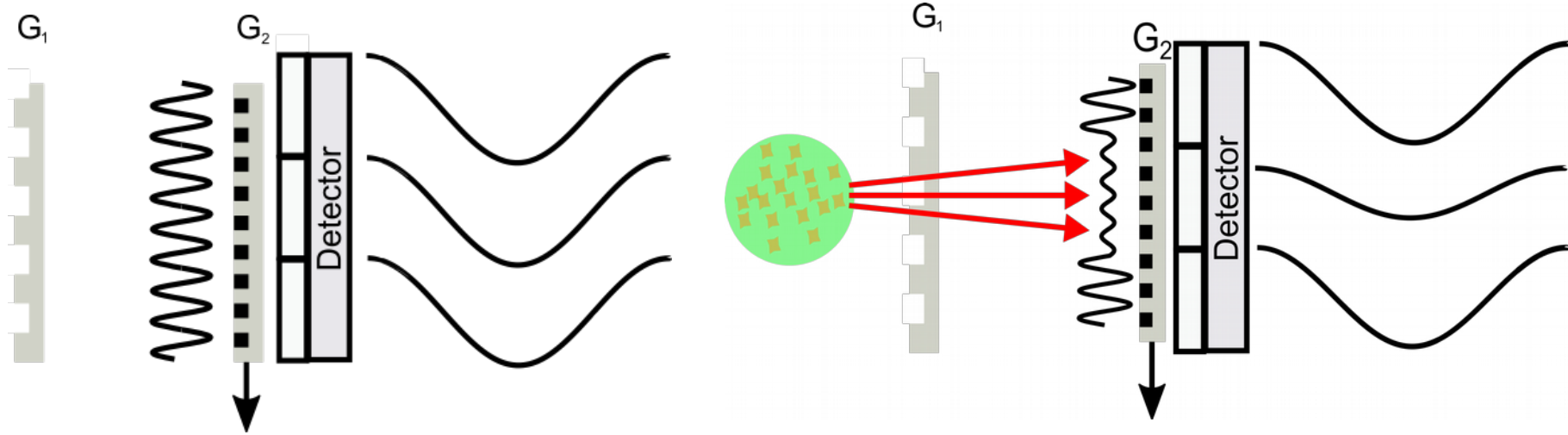


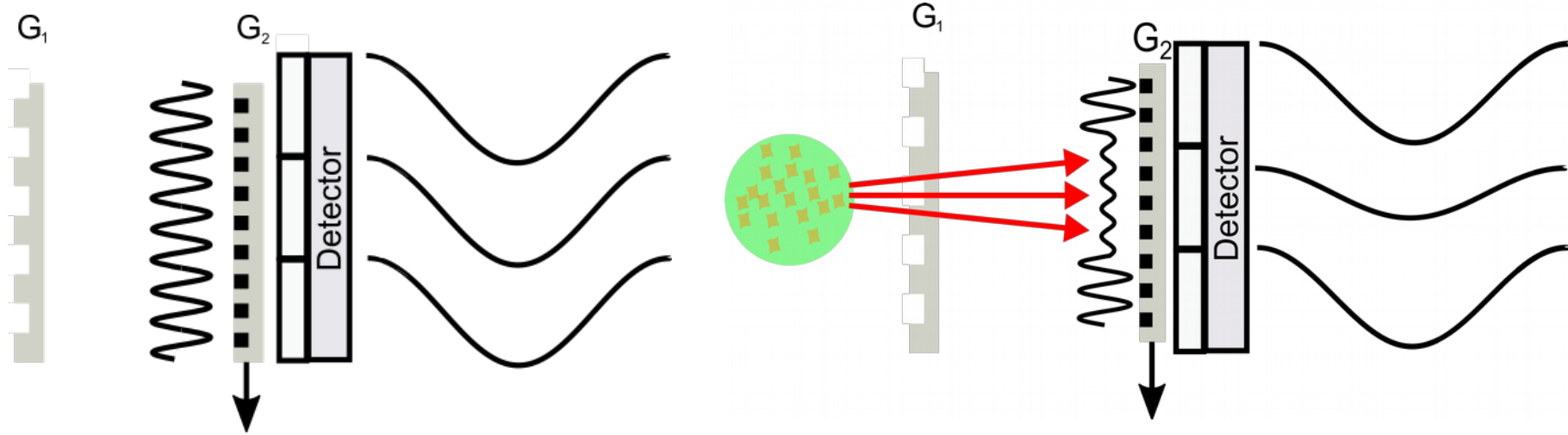




- Intensity modulation generated by G_1 cannot be resolved with standard imaging detectors

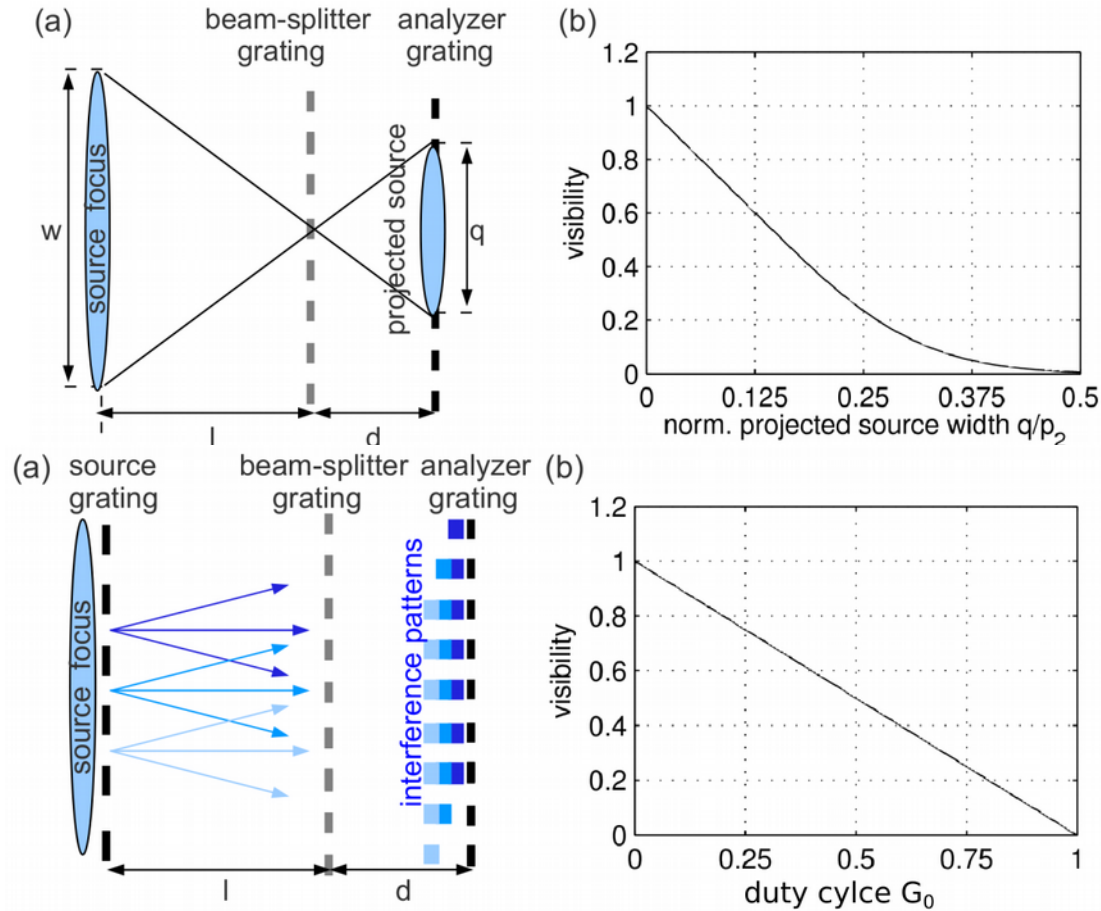




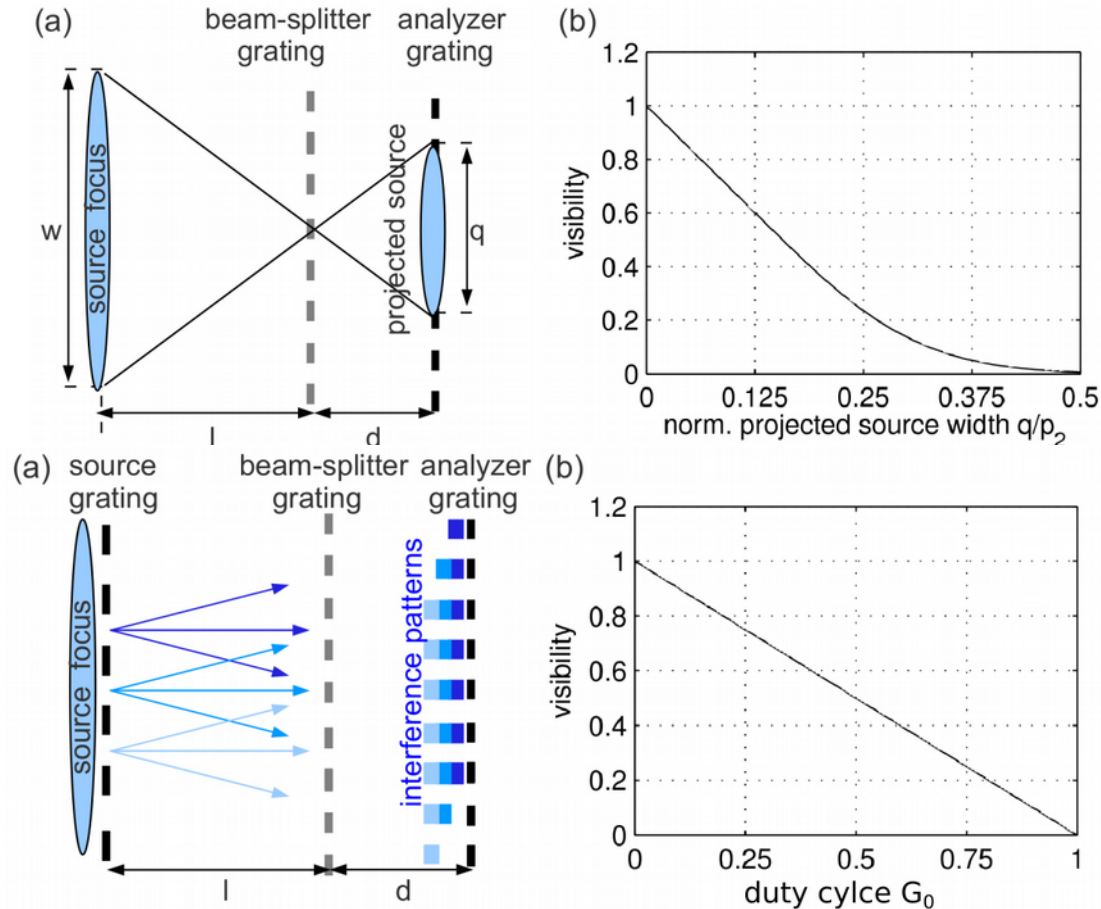


- By using an absorption grating (G₂), with the same period as the interference pattern, the pattern can be analysed
- Period of G₂ used in ANTARES $\approx 4 \mu\text{m}$

G0 – providing spatial coherence



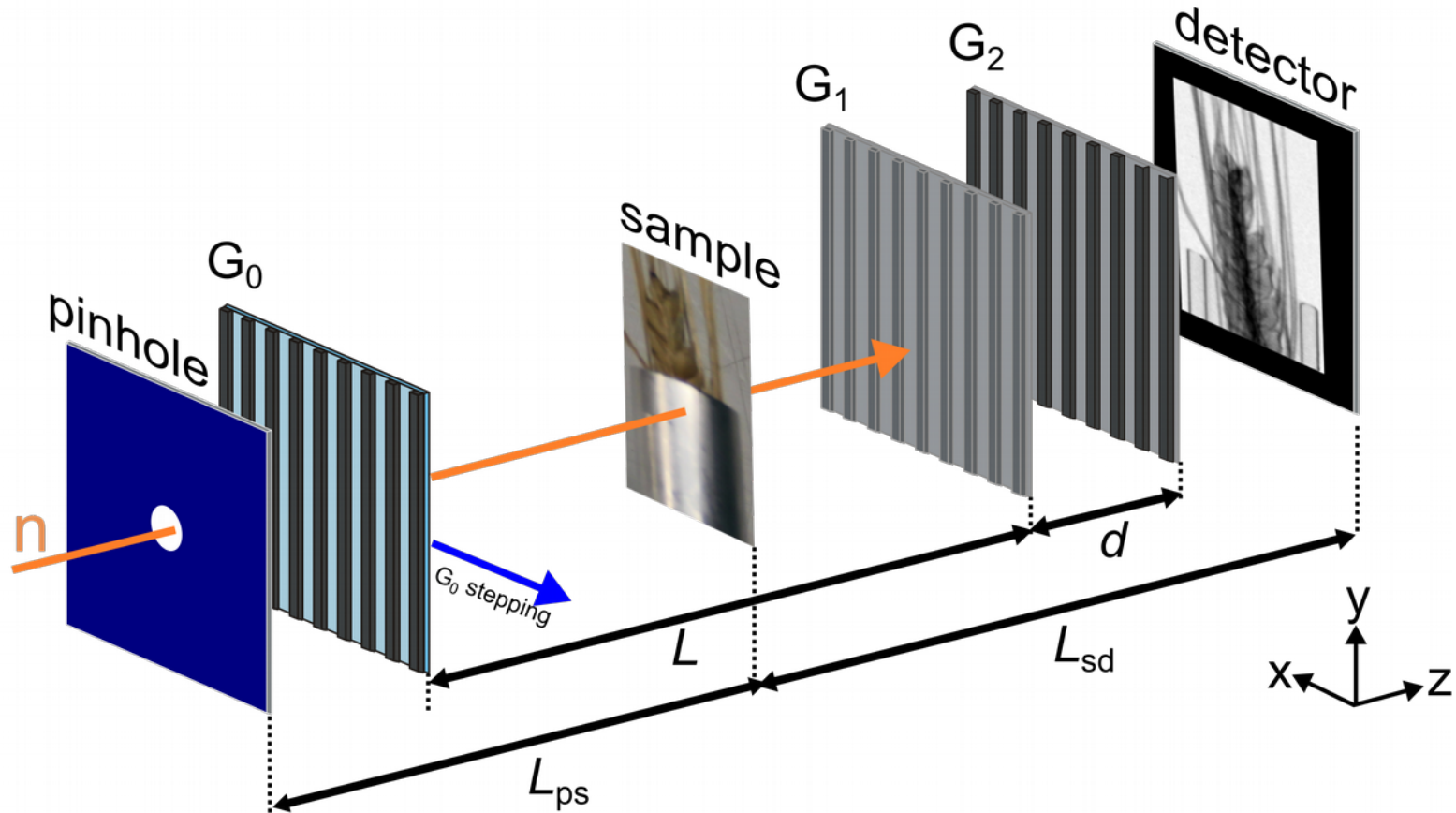
Contributions to the characterization of grating-based x-ray phase-contrast imaging, M. Chabior, Thesis, 2011



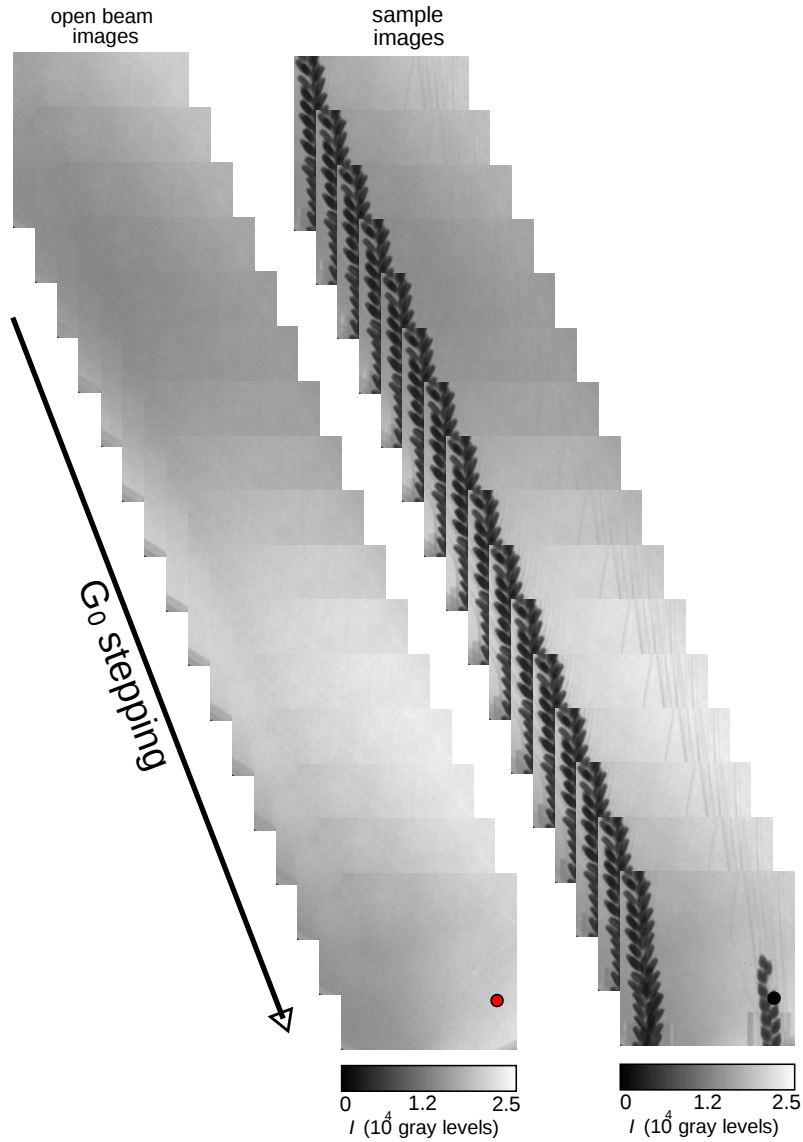
Contributions to the characterization of grating-based x-ray phase-contrast imaging, M. Chabior, Thesis, 2011

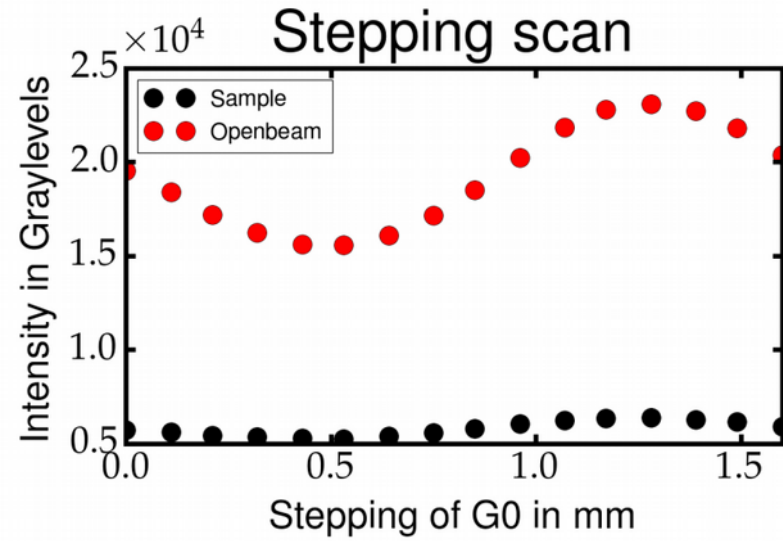
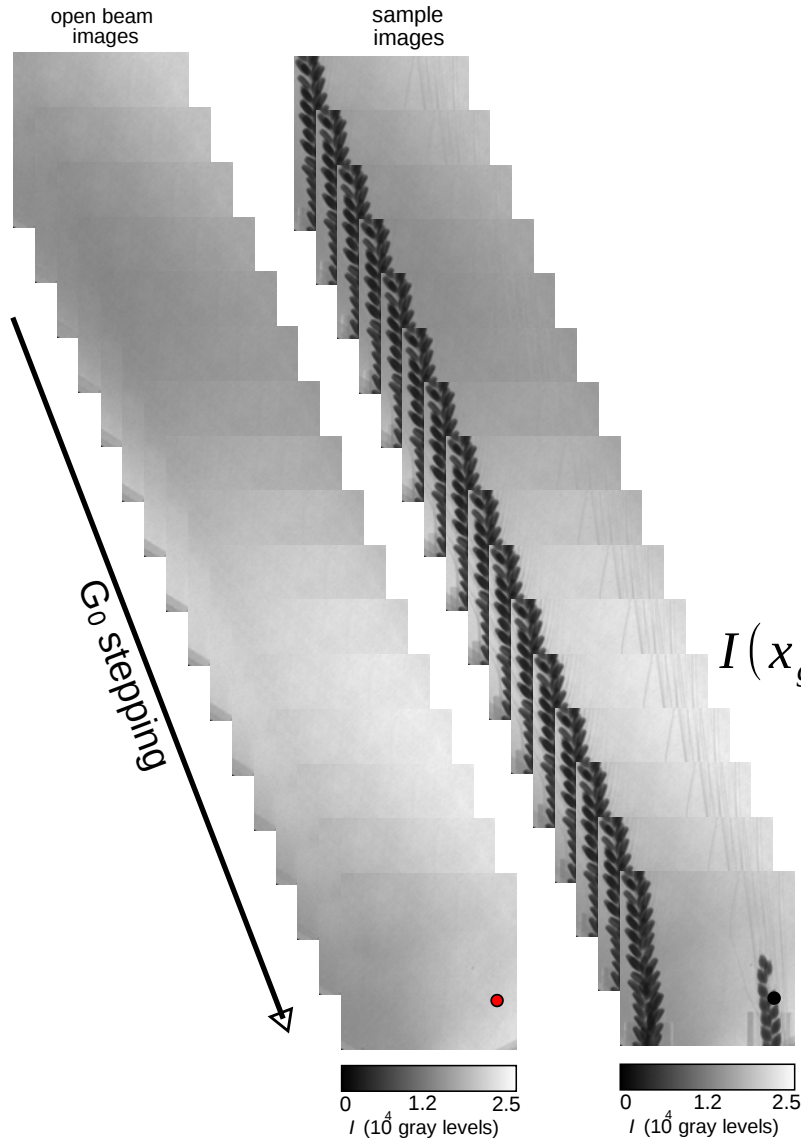
- G0 needed to keep a reasonable compromise between flux and visibility
- Constructive overlap of the interference patterns

Neutron grating interferometer

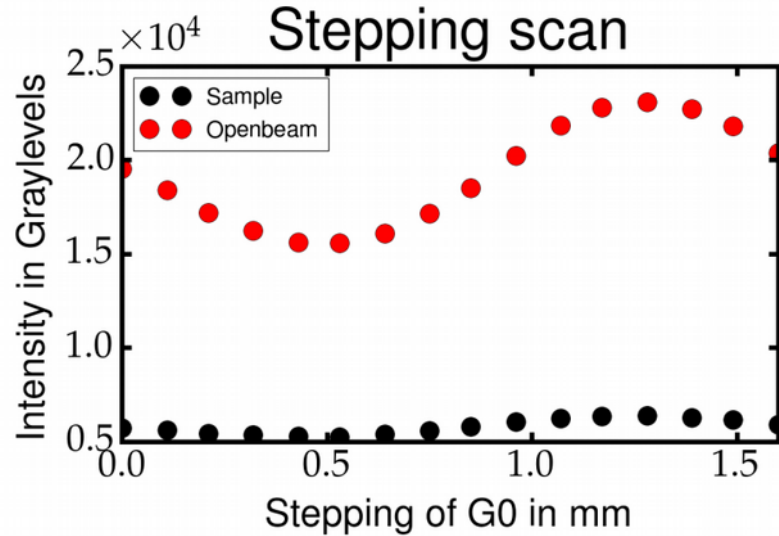
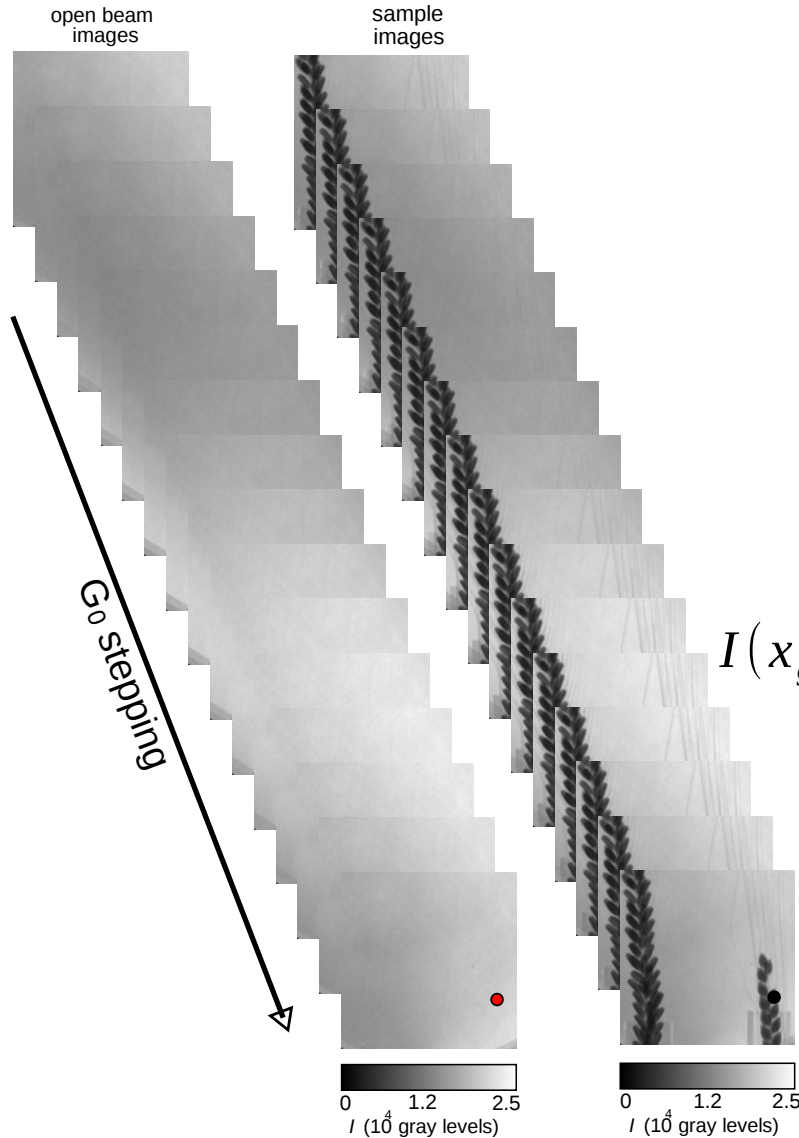


Performing measurements



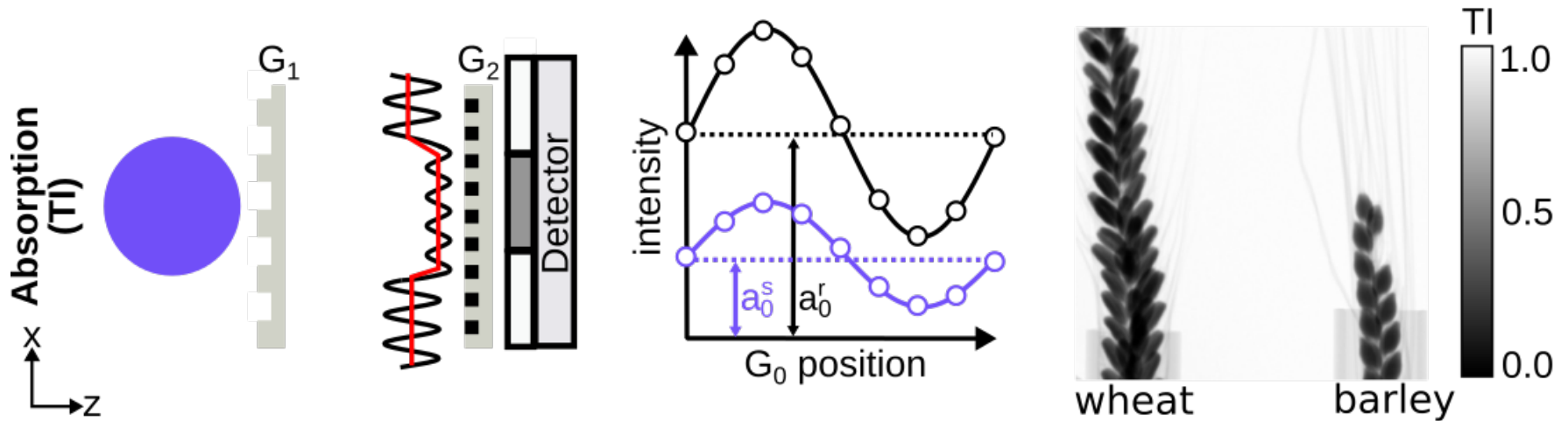


$$I(x_{gi}, m, n) = a_0(m, n) + a_1(m, n) \cos\left(\frac{2\pi x_{gi}}{p_i} - \varphi(m, n)\right)$$



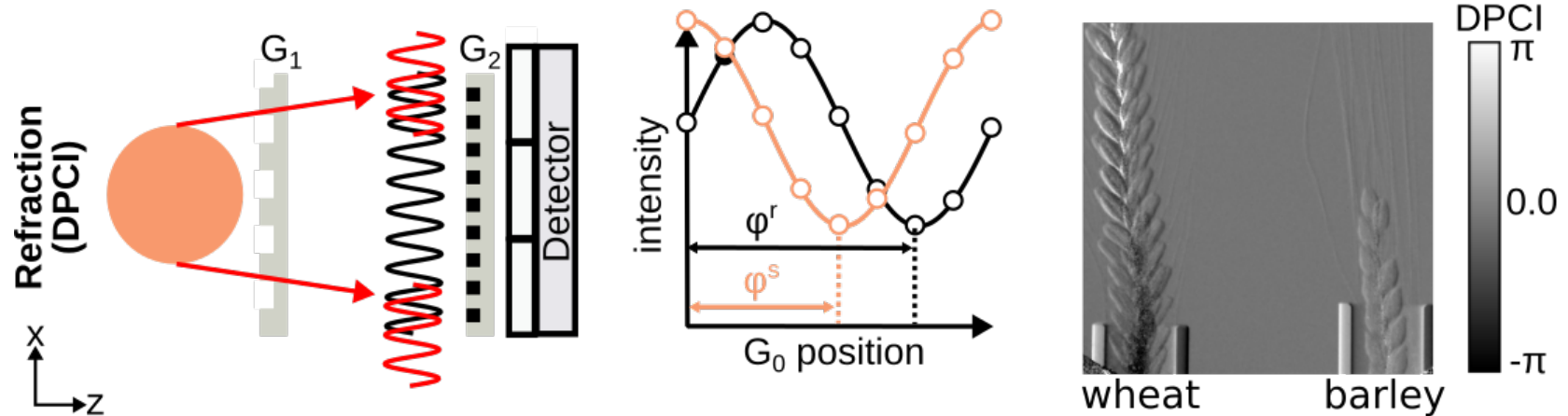
$$I(x_{gi}, m, n) = a_0(m, n) + a_1(m, n) \cos\left(\frac{2\pi x_{gi}}{p_i} - \varphi(m, n)\right)$$

- Movement of any of the three gratings generates an intensity oscillation in every pixel
- Analysis of the oscillation and comparison between open beam and sample allows to obtain information about the sample



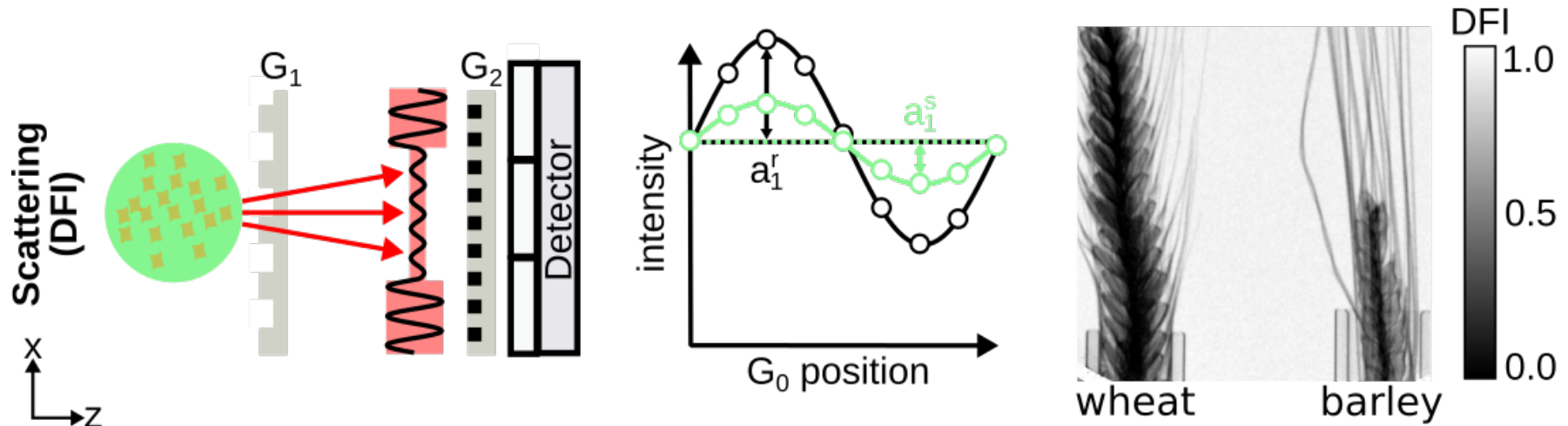
$$TI = \frac{a_0^s}{a_0^r}$$

- Transmission image (TI) is equal to the image of monochromatic radiography



$$DPCI = \varphi^s - \varphi^r$$

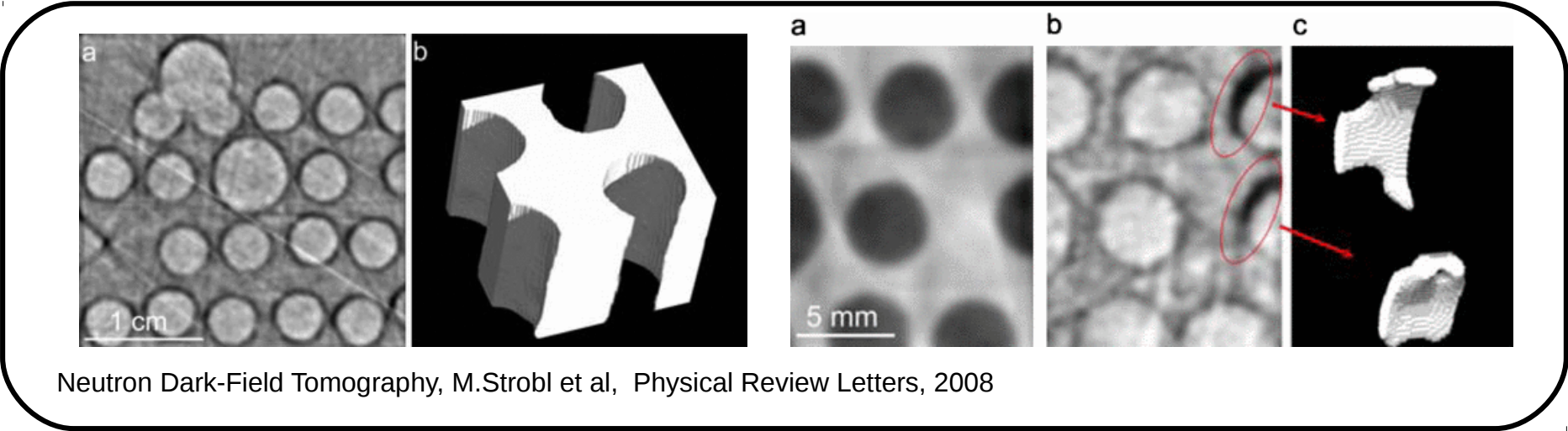
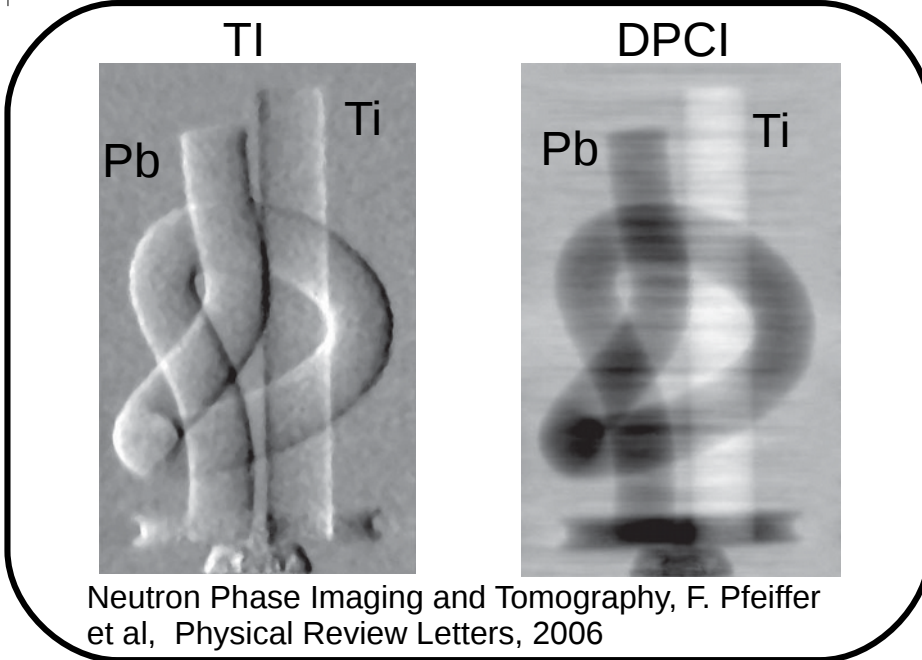
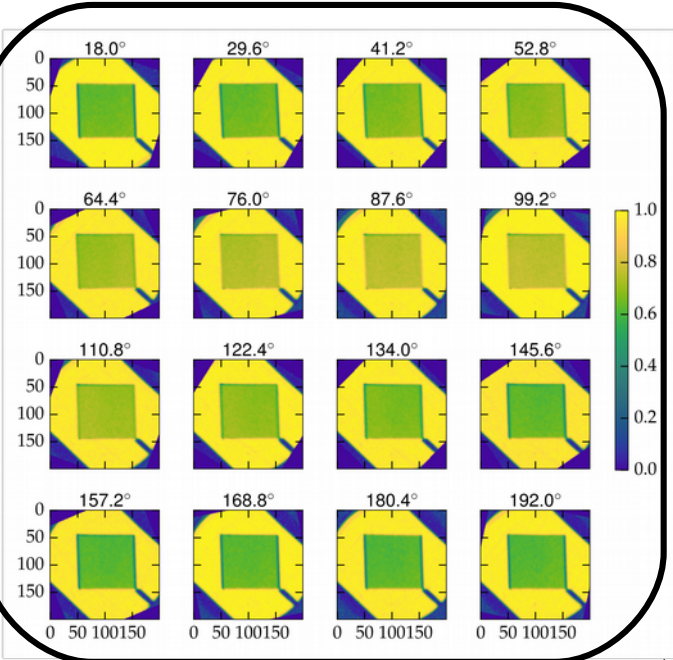
- DPCI maps the gradient of the neutron phase introduced by the sample
- Only sensitive perpendicular to the grating lines
- Currently rarely used in nGI as it delivers no additional information

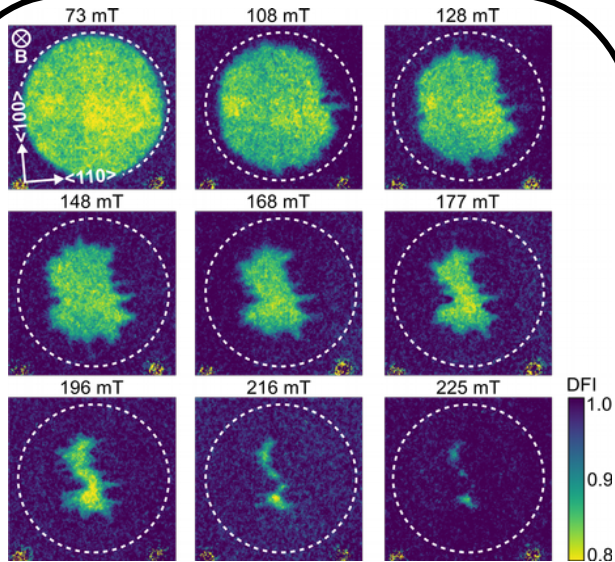


$$DFI = \frac{V^s}{V^r} = \frac{a_1^s \cdot a_0^r}{a_0^s \cdot a_1^r}$$

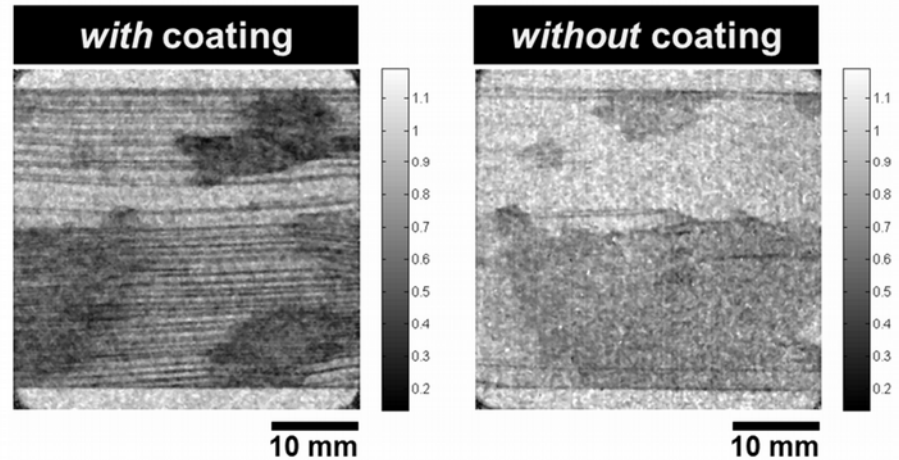
- DFI maps areas containing structures in the range of 100 nm to 15 μm
- Contrast is generated by USANS destroying the interference pattern
- Also sensitive to scattering off magnetic structures

Examples for nGI measurements





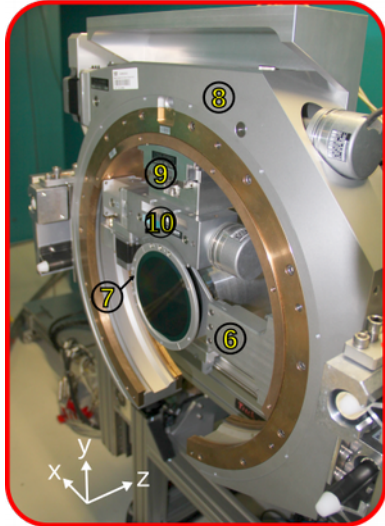
Vortex matter beyond SANS, T. Reimann, Thesis, 2017



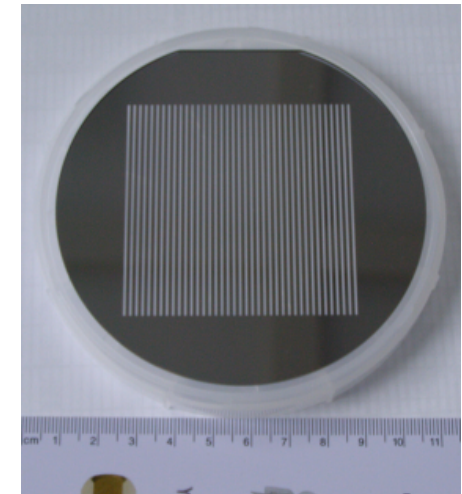
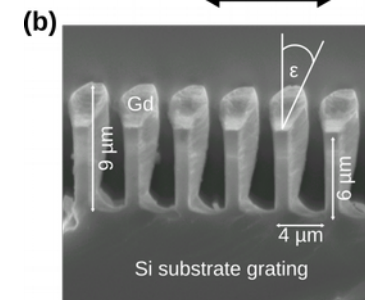
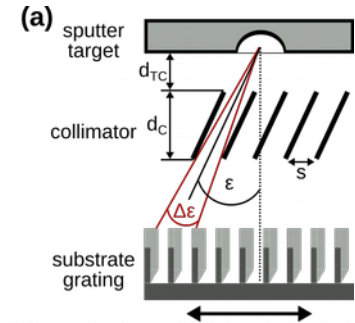
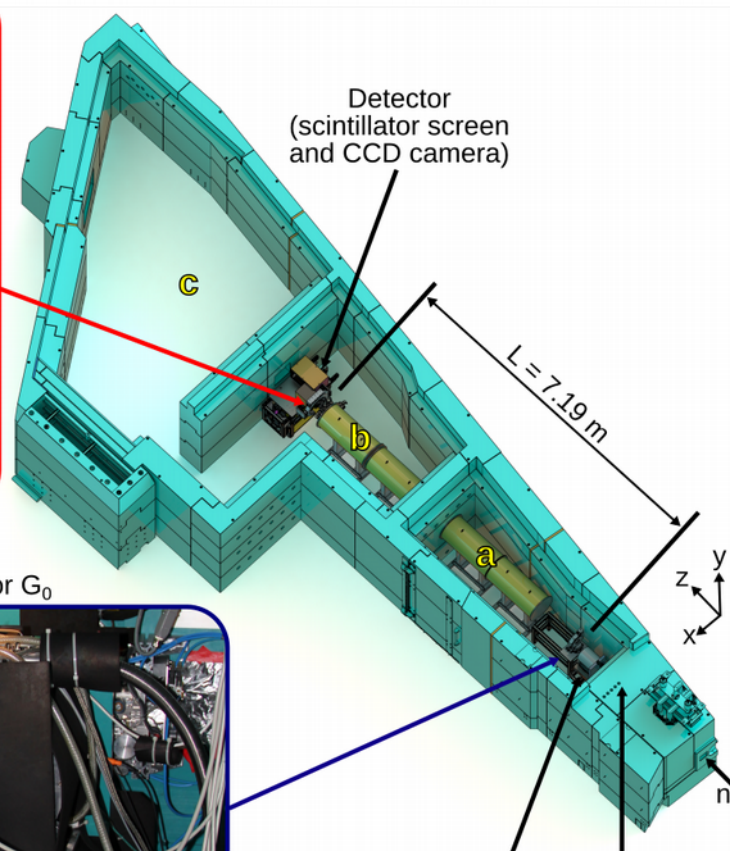
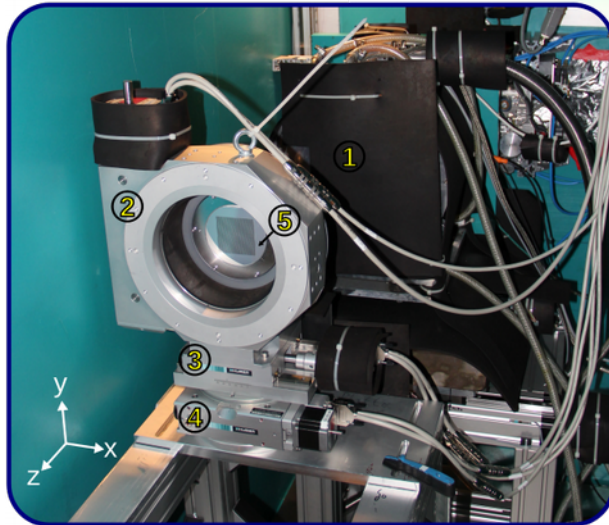
Determination of Bulk Magnetic Volume Properties by Neutron Dark-Field Imaging, Ch. Grünzweig et al, 10 WCNR, 2014

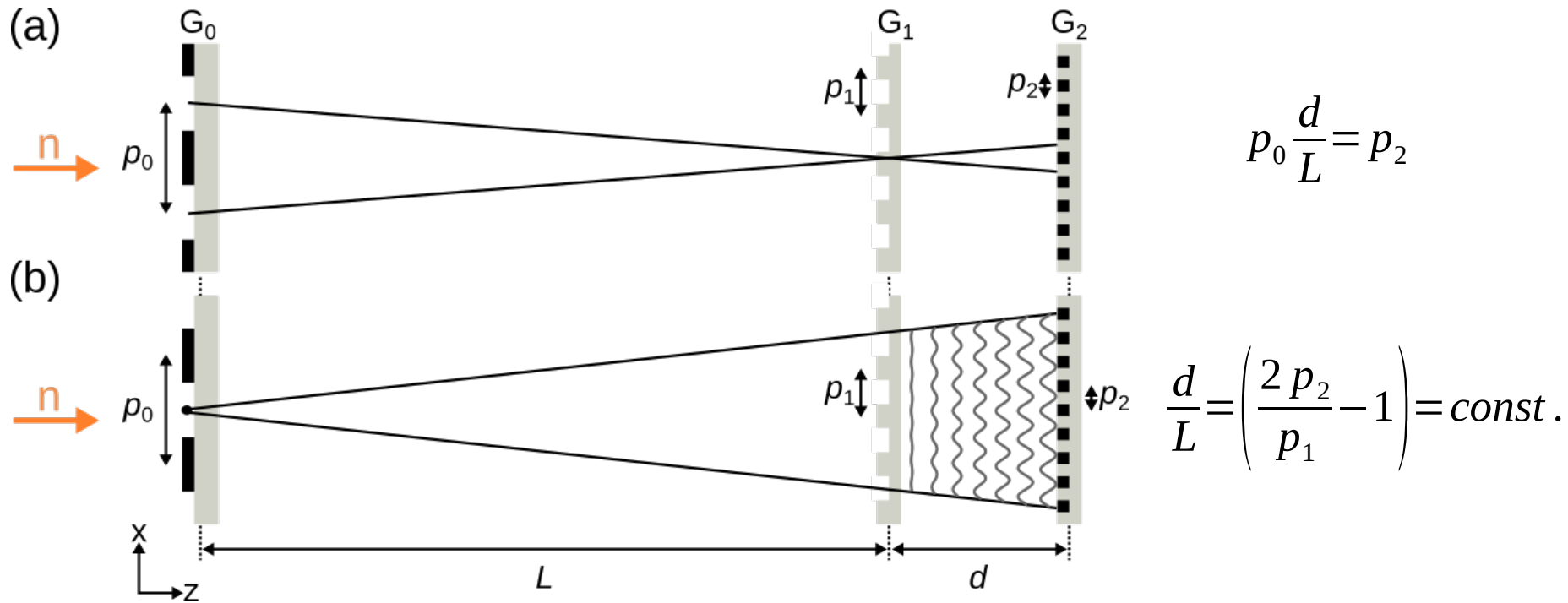
Construction of an nGI

Euler cradle for G_1 & G_2

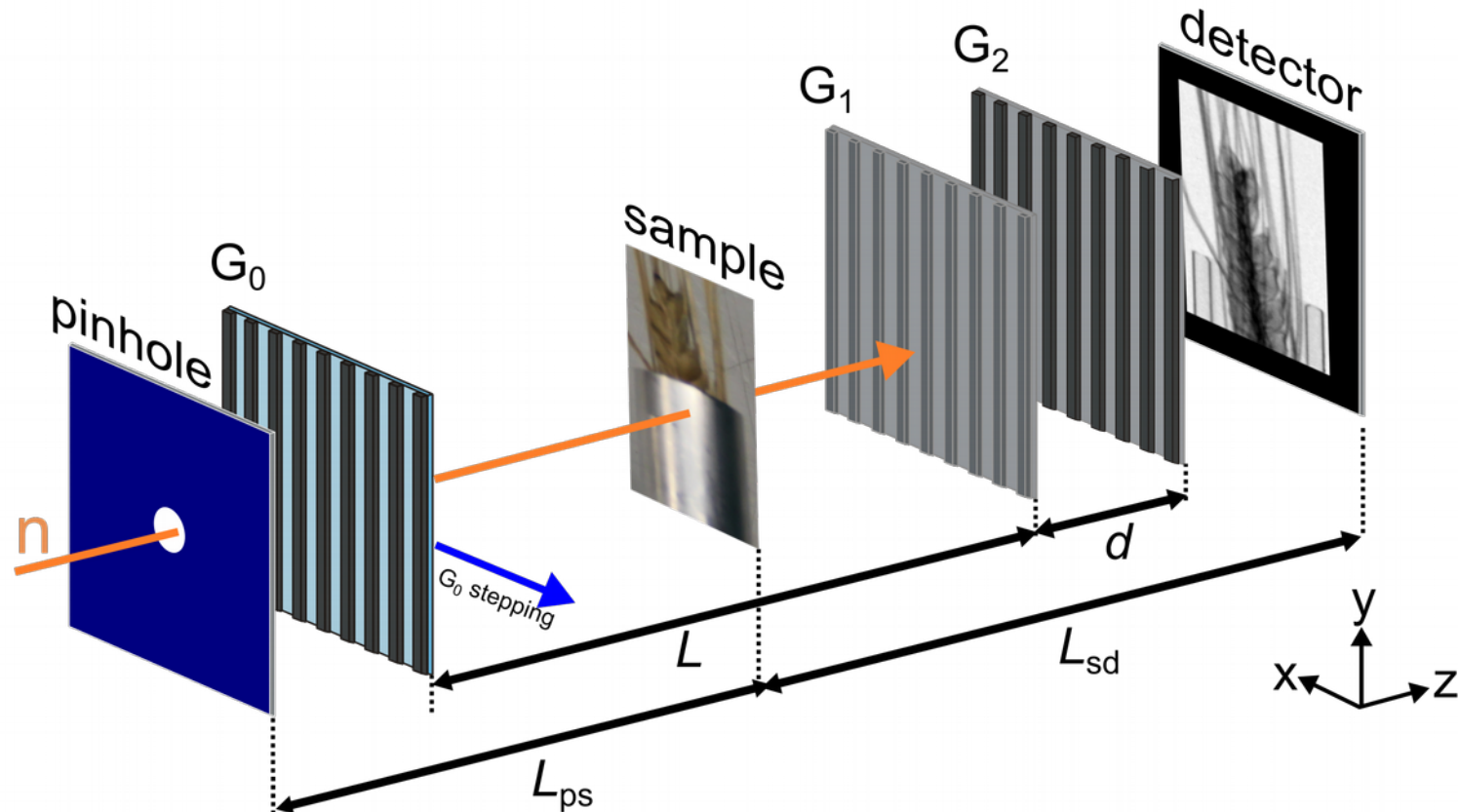


Rotation stage for G_0





- Strong geometric constraints imposed by the nGI
- Change of one component leads to a change in the whole setup
- Correlation length defined by these geometric constraints
- Positioning of the gratings key to good results



- nGI (DFI) allows to look at USANS in samples, with which structures in the range of 100 nm to 15 μm can be probed
- Magnetic structures can also be resolved by this, as neutrons scatter on the domain walls
- Compared to normal USANS lower q -range, but allows for spatial resolution

Thank you for your attention!

Questions?